

# Post-quantum key exchange for the Internet

---

**Douglas Stebila**  McMaster  
University

# Acknowledgements

## Collaborators

- Joppe Bos
- Craig Costello and Michael Naehrig
- Léo Ducas
- Ilya Mironov and Ananth Raghunathan
- Michele Mosca
- Valeria Nikolaenko



## Support

- Australian Research Council (ARC)
- Natural Sciences and Engineering Research Council of Canada (NSERC)
- Queensland University of Technology
- Tutte Institute for Mathematics and Computing

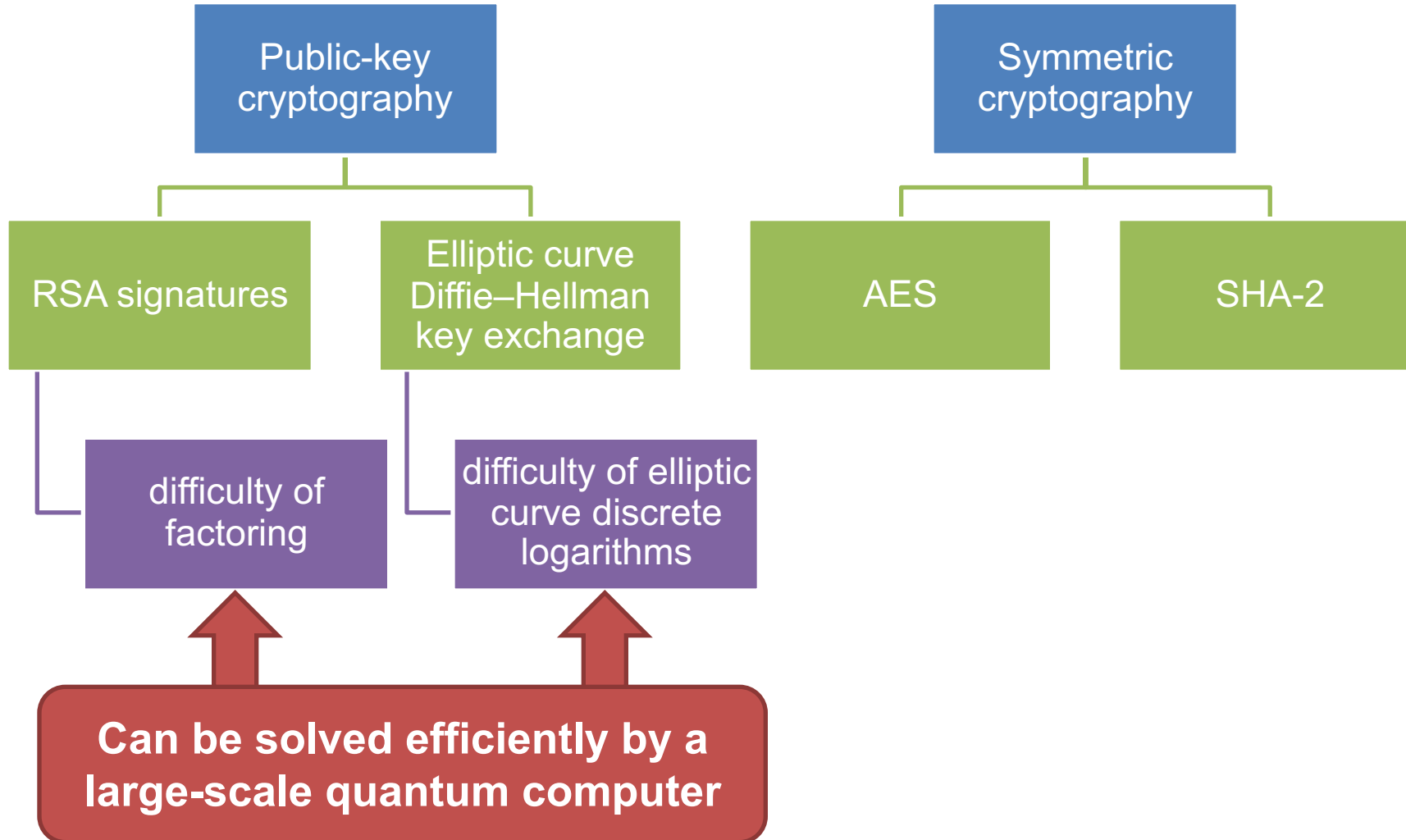


# Motivation

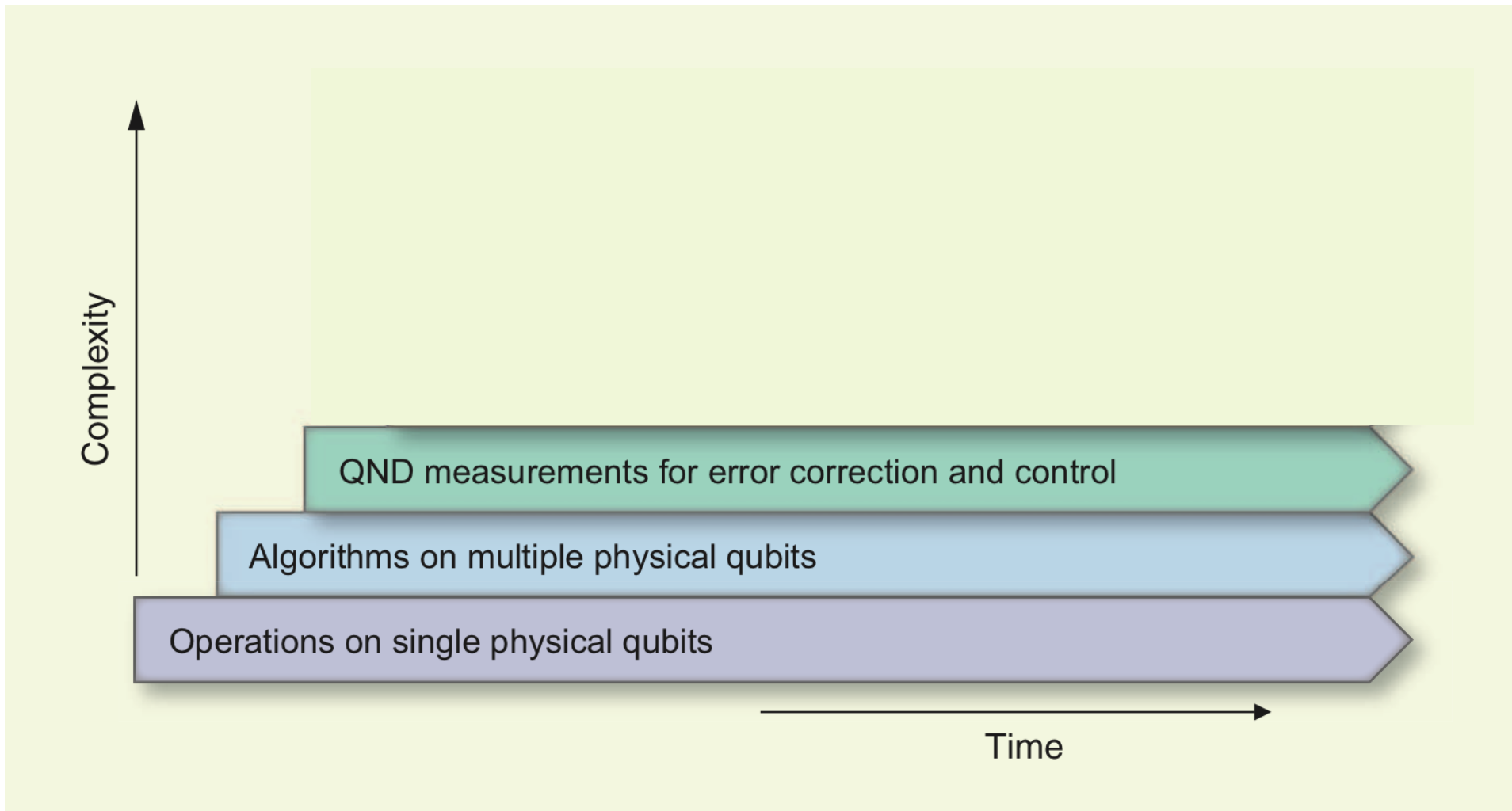
---

# Contemporary cryptography

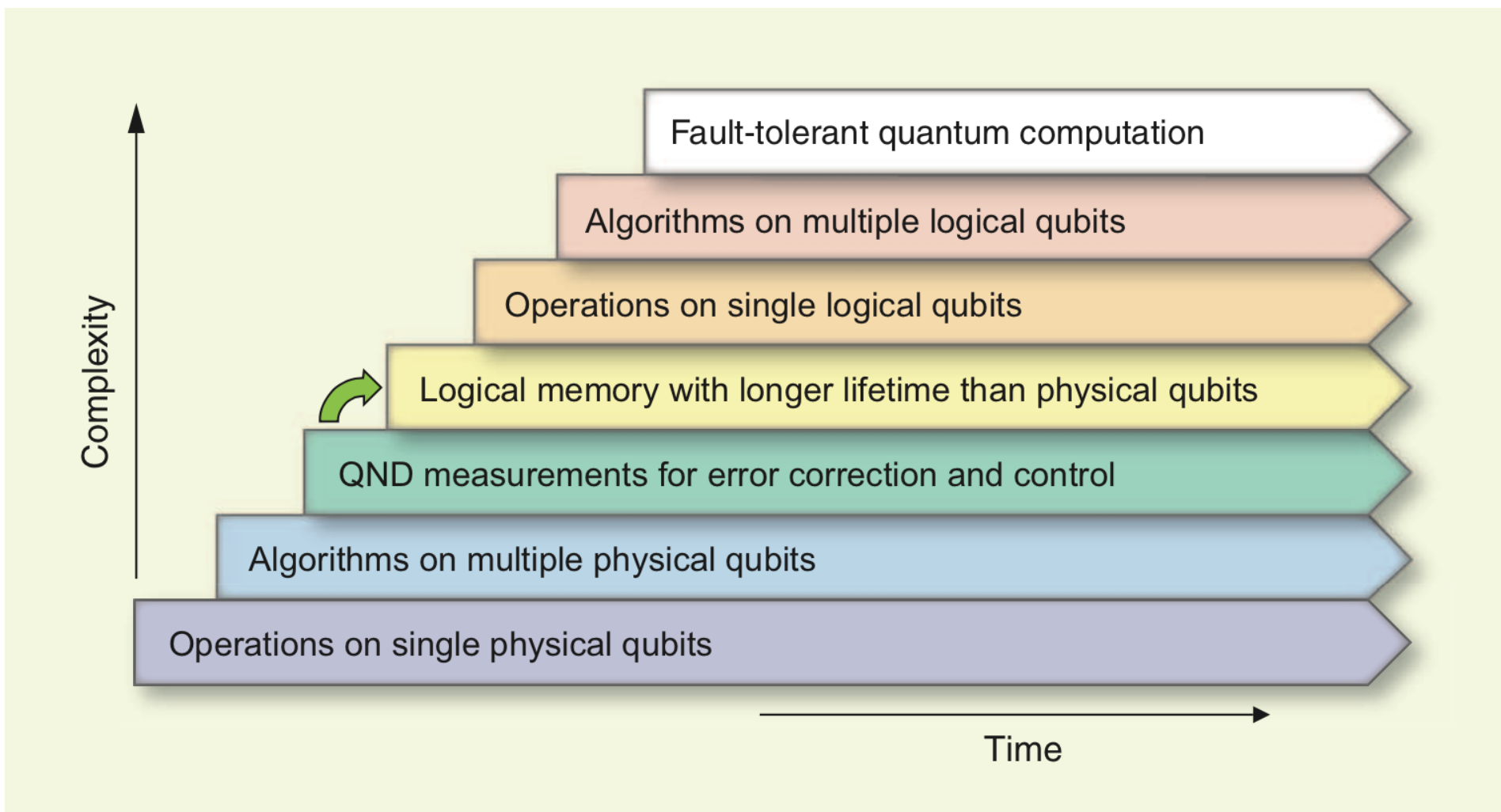
TLS-ECDHE-RSA-AES128-GCM-SHA256



# Building quantum computers



# Building quantum computers



# When will a large-scale quantum computer be built?

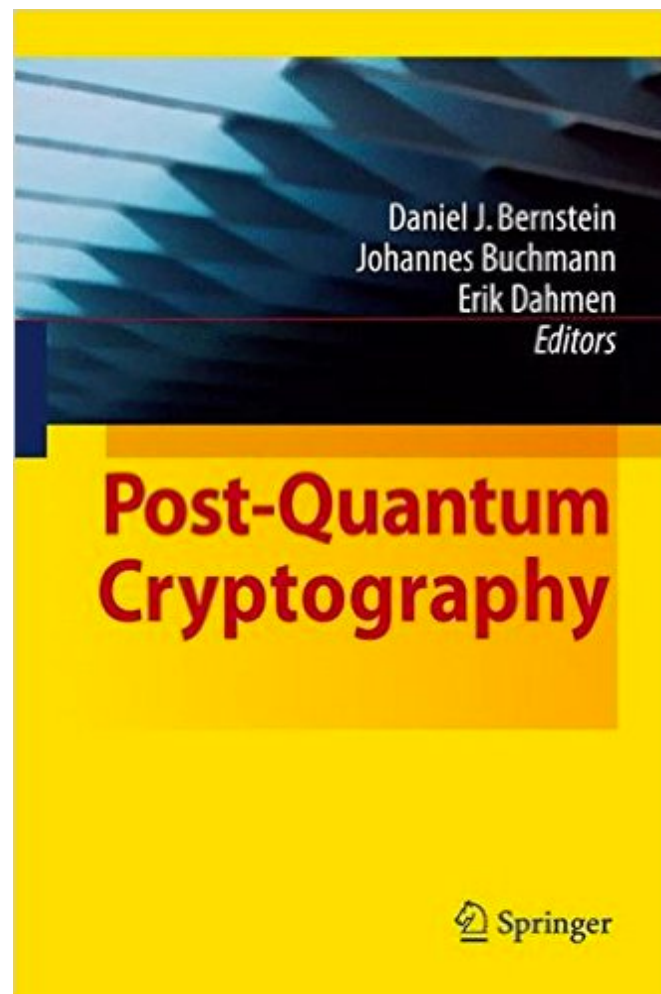
“I estimate a  $1/7$  chance of breaking RSA-2048 by 2026 and a  $1/2$  chance by 2031.”

— Michele Mosca, November 2015  
<https://eprint.iacr.org/2015/1075>

# Post-quantum cryptography in academia

## Conference series

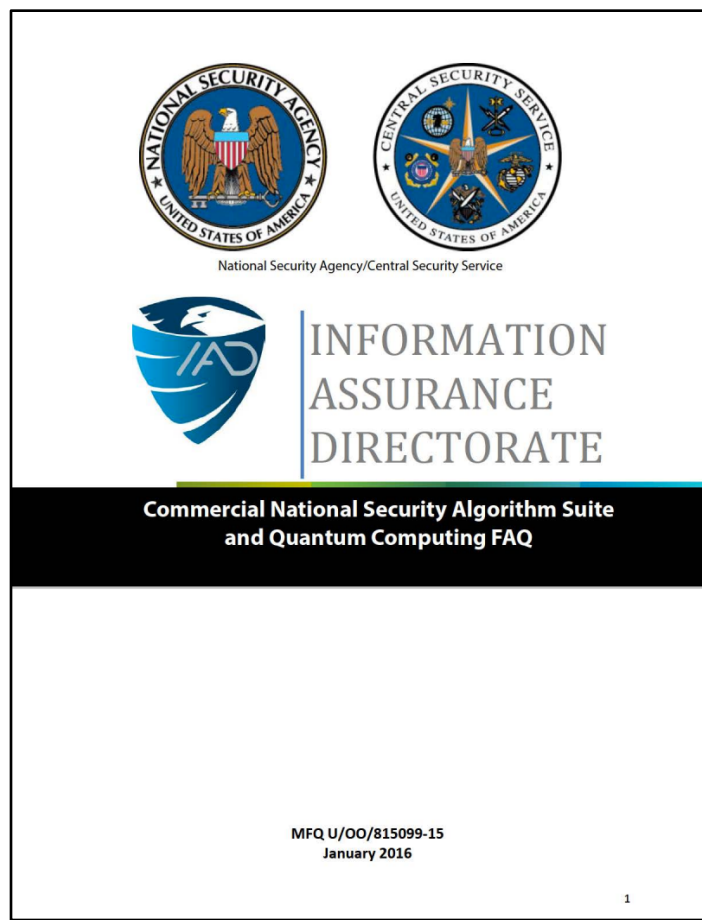
- PQCrypto 2006
- PQCrypto 2008
- PQCrypto 2010
- PQCrypto 2011
- PQCrypto 2013
- PQCrypto 2014
- PQCrypto 2016



2009



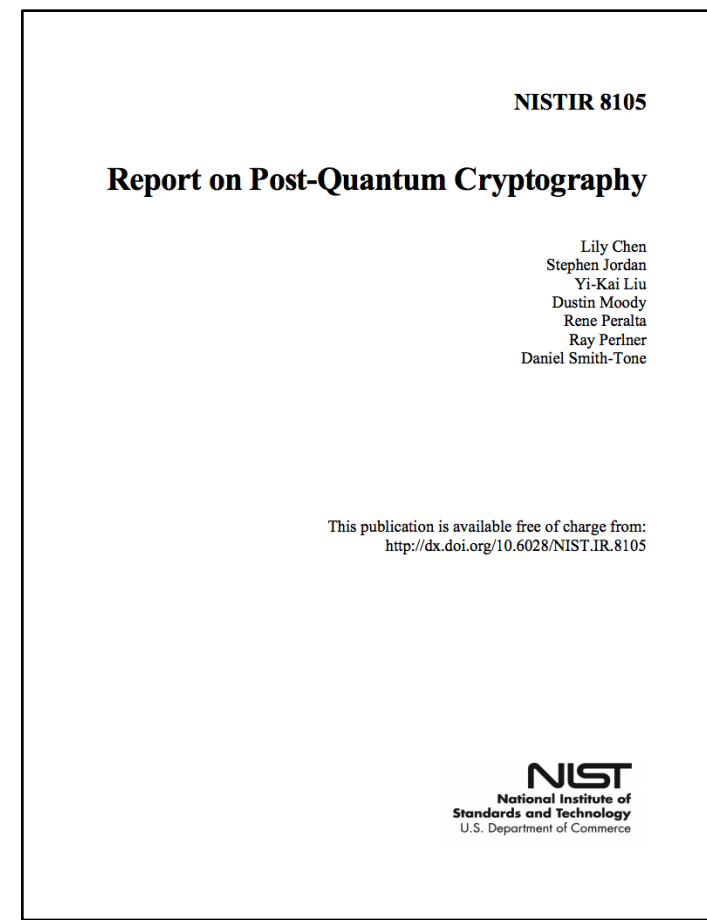
# Post-quantum cryptography in government



Aug. 2015 (Jan. 2016)

“IAD will initiate a transition to quantum resistant algorithms in the not too distant future.”

– NSA Information Assurance Directorate,  
Aug. 2015



Apr. 2016

# NIST Post-quantum Crypto Project timeline

<b>September 16, 2016</b>	<b>Feedback on call for proposals</b>
Fall 2016	Formal call for proposals
November 2017	Deadline for submissions
Early 2018	Workshop – submitters' presentations
3-5 years	Analysis phase
2 years later	Draft standards ready

<http://www.nist.gov/pqcrypto>

# Post-quantum / quantum-safe crypto

No known exponential quantum speedup

## Hash-based

- Merkle signatures
- Sphincs

## Code-based

- McEliece

## Multivariate

- multivariate quadratic

## Lattice-based

- NTRU
- learning with errors
- ring-LWE

## Isogenies

- supersingular elliptic curve isogenies

# Lots of questions

- Design better post-quantum key exchange and signature schemes
- Improve classical and quantum attacks
- Pick parameter sizes
- Develop fast, secure implementations
- Integrate them into the existing infrastructure

# This talk

- Two key exchange protocols from lattice-based problems
  - BCNS15: key exchange from the ring learning with errors problem
  - Frodo: key exchange from the learning with errors problem
- Open Quantum Safe project
  - A library for comparing post-quantum primitives
  - Framework for easing integration into applications like OpenSSL

# Why key exchange?

**Premise:** large-scale quantum computers don't exist right now, but we want to protect today's communications against tomorrow's adversary.

- Signatures still done with traditional primitives (RSA/ECDSA)
  - we only need authentication to be secure *now*
  - benefit: use existing RSA-based PKI
- Key agreement done with ring-LWE, LWE, ...
  - Also consider “hybrid” ciphersuites that use post-quantum and traditional elliptic curve

# Learning with errors problems

---

# Solving systems of linear equations

$$\begin{matrix} \mathbb{Z}_{13}^{7 \times 4} \\ \begin{array}{|c|c|c|c|} \hline 4 & 1 & 11 & 10 \\ \hline 5 & 5 & 9 & 5 \\ \hline 3 & 9 & 0 & 10 \\ \hline 1 & 3 & 3 & 2 \\ \hline 12 & 7 & 3 & 4 \\ \hline 6 & 5 & 11 & 4 \\ \hline 3 & 3 & 5 & 0 \\ \hline \end{array} \end{matrix} \times \begin{matrix} \text{secret} \\ \mathbb{Z}_{13}^{4 \times 1} \\ \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \end{array} \end{matrix} = \begin{matrix} \mathbb{Z}_{13}^{7 \times 1} \\ \begin{array}{|c|} \hline 4 \\ \hline 8 \\ \hline 1 \\ \hline 10 \\ \hline 4 \\ \hline 12 \\ \hline 9 \\ \hline \end{array} \end{matrix}$$

Linear system problem: given **blue**, find **red**



# Solving systems of linear equations

$$\begin{matrix} \mathbb{Z}_{13}^{7 \times 4} & \text{secret} \\ & \mathbb{Z}_{13}^{4 \times 1} & & \mathbb{Z}_{13}^{7 \times 1} \end{matrix}$$

4	1	11	10
5	5	9	5
3	9	0	10
1	3	3	2
12	7	3	4
6	5	11	4
3	3	5	0

×

6
9
11
11

=

4
8
1
10
4
12
9

Easily solved using  
Gaussian elimination  
(Linear Algebra 101)

Linear system problem: given **blue**, find **red**

# Learning with errors problem

random  $\mathbb{Z}_{13}^{7 \times 4}$       secret  $\mathbb{Z}_{13}^{4 \times 1}$       small noise  $\mathbb{Z}_{13}^{7 \times 1}$        $\mathbb{Z}_{13}^{7 \times 1}$

4	1	11	10	×	+	=	4		
5	5	9	5				6	-1	7
3	9	0	10				9	1	2
1	3	3	2				11	1	11
12	7	3	4				11	1	5
6	5	11	4					0	12
3	3	5	0					-1	8

# Learning with errors problem

random  $\mathbb{Z}_{13}^{7 \times 4}$       secret  $\mathbb{Z}_{13}^{4 \times 1}$       small noise  $\mathbb{Z}_{13}^{7 \times 1}$        $\mathbb{Z}_{13}^{7 \times 1}$

4	1	11	10
5	5	9	5
3	9	0	10
1	3	3	2
12	7	3	4
6	5	11	4
3	3	5	0

×

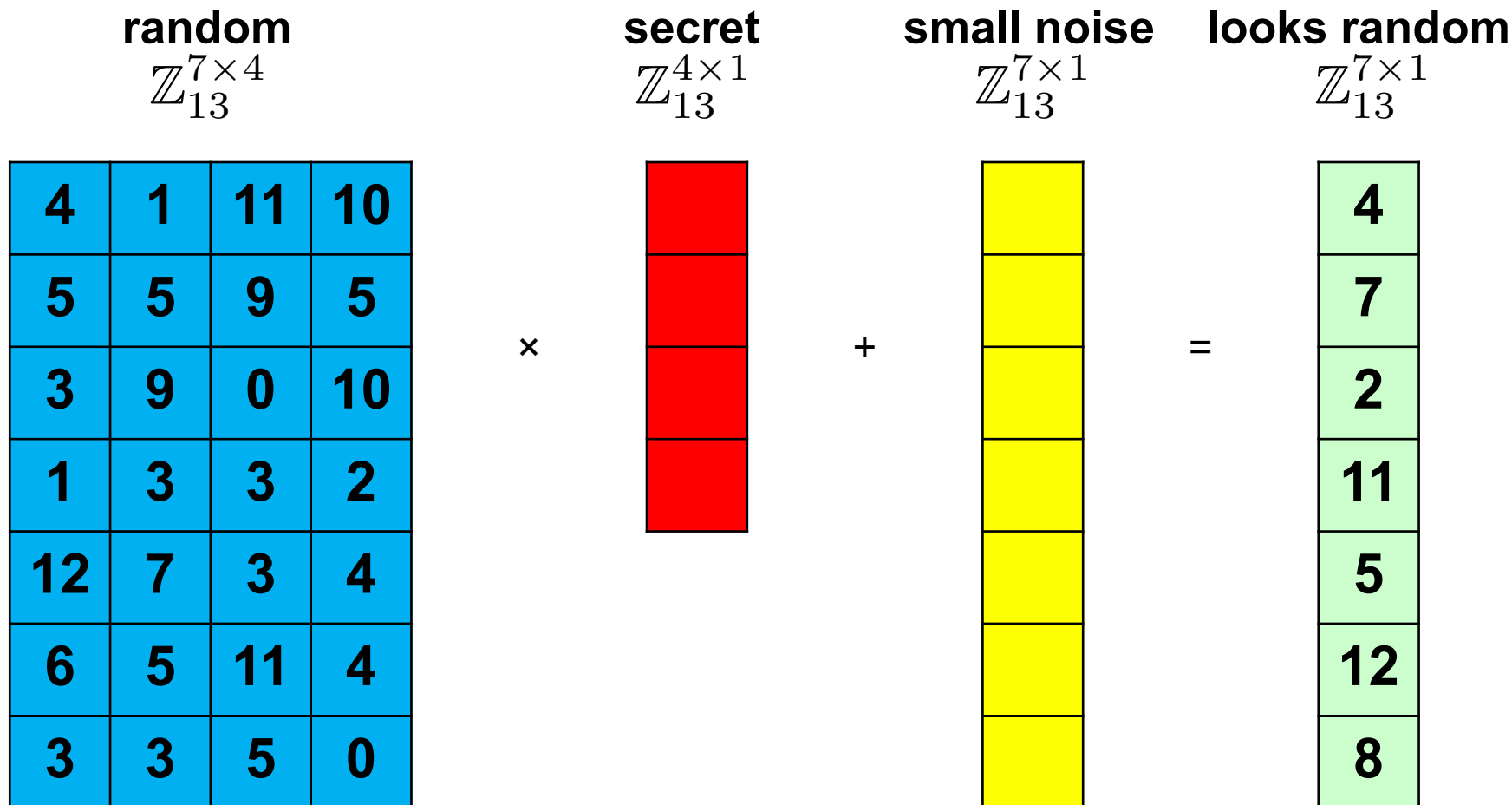

+


=

4
7
2
11
5
12
8

Computational LWE problem: given **blue**, find **red**

# Decision learning with errors problem



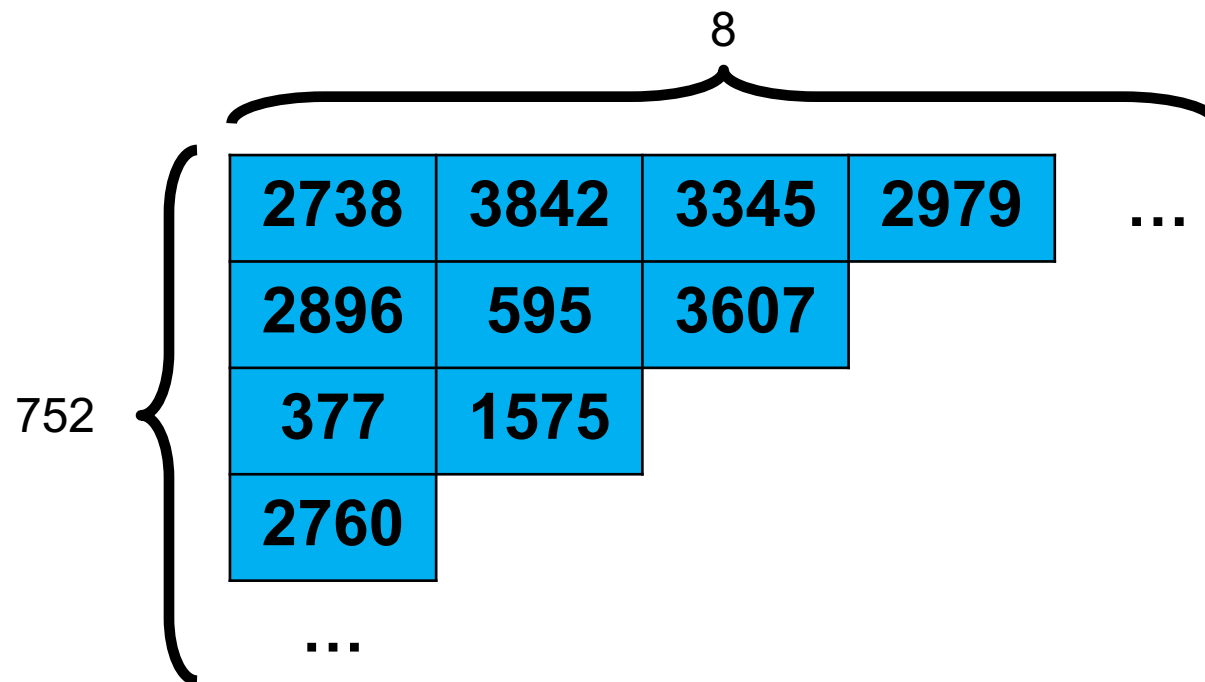
Decision LWE problem: given **blue**, distinguish **green** from random

# Toy example versus real-world example

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
5	5	9	5
3	9	0	10
1	3	3	2
12	7	3	4
6	5	11	4
3	3	5	0

$$\mathbb{Z}_{2^{15}}^{752 \times 8}$$



$$752 \times 28 \times 15 \text{ bits} = 11 \text{ KiB}$$

# Ring learning with errors problem

random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
10	4	1	11
11	10	4	1
1	11	10	4
4	1	11	10
10	4	1	11
11	10	4	1

Each row is the cyclic shift of the row above

# Ring learning with errors problem

random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
3	4	1	11
2	3	4	1
12	2	3	4
9	12	2	3
10	9	12	2
11	10	9	12

Each row is the cyclic  
shift of the row above

...

with a special wrapping rule:  
 $x$  wraps to  $-x \pmod{13}$ .

# Ring learning with errors problem

random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
---	---	----	----

Each row is the cyclic shift of the row above

...

with a special wrapping rule:  
 $x$  wraps to  $-x \pmod{13}$ .

So I only need to tell you the first row.



# Ring learning with errors problem

$$\mathbb{Z}_{13}[x]/\langle x^4 + 1 \rangle$$

$$4 + 1x + 11x^2 + 10x^3$$

random

$$\times \quad 6 + 9x + 11x^2 + 11x^3$$

secret

$$+ \quad 0 - 1x + 1x^2 + 1x^3$$

small noise

---

$$= \quad 10 + 5x + 10x^2 + 7x^3$$

# Ring learning with errors problem

$$\mathbb{Z}_{13}[x]/\langle x^4 + 1 \rangle$$

$$4 + 1x + 11x^2 + 10x^3$$

random

×



secret

+



small noise

=

$$10 + 5x + 10x^2 + 7x^3$$

Computational ring-LWE problem: given **blue**, find **red**

# Decision ring learning with errors problem

$$\mathbb{Z}_{13}[x]/\langle x^4 + 1 \rangle$$

$$4 + 1x + 11x^2 + 10x^3$$

random

×



secret

+



small noise

=

$$10 + 5x + 10x^2 + 7x^3$$

looks random

**Decision ring-LWE problem:** given **blue**, distinguish **green** from random

# Decision ring learning with errors problem with small secrets

$$\mathbb{Z}_{13}[x]/\langle x^4 + 1 \rangle$$

$$4 + 1x + 11x^2 + 10x^3$$

random

×

$$1 + 0x - 1x^2 + 2x^3$$

small secret

+

$$\text{small noise}$$

small noise

=

$$10 + 5x + 10x^2 + 7x^3$$

looks random

**Decision ring-LWE problem:** given **blue**, distinguish **green** from random

# Problems

[Reg05] Regev, *STOC 2005*; *J. ACM 2009*.

Computational  
LWE problem

Decision  
LWE problem

with or without  
short secrets

Computational  
ring-LWE problem

Decision  
ring-LWE problem

[LPR10] Lyubashevsky, Piekert, Regev. *EUROCRYPT 2010*.

# Key agreement from ring-LWE

---

Bos, Costello, Naehrig, Stebila.

Post-quantum key exchange for the TLS protocol from the ring learning with errors problem.

*IEEE Symposium on Security & Privacy (S&P) 2015.*

<https://www.douglas.stebila.ca/research/papers/SP-BCNS15/>

# Decision ring learning with errors problem with short secrets

**Definition.** Let  $n$  be a power of 2,  $q$  be a prime, and  $R_q = \mathbb{Z}_q[X]/(X^n + 1)$  be the ring of polynomials in  $X$  with integer coefficients modulo  $q$  and polynomial reduction modulo  $X^n + 1$ . Let  $\chi$  be a distribution over  $R_q$ .

Let  $s \stackrel{\$}{\leftarrow} \chi$ .

Define:

- $O_{\chi,s}$ : Sample  $a \stackrel{\$}{\leftarrow} \mathcal{U}(R_q)$ ,  $e \stackrel{\$}{\leftarrow} \chi$ ; return  $(a, as + e)$ .
- $U$ : Sample  $(a, b') \stackrel{\$}{\leftarrow} \mathcal{U}(R_q \times R_q)$ ; return  $(a, b')$ .

The *decision R-LWE problem with short secrets* for  $n, q, \chi$  is to distinguish  $O_{\chi,s}$  from  $U$ .

# Hardness of decision ring-LWE

worst-case approximate shortest  
(independent) vector problem  
(SVP/SIVP) on ideal lattices in  $R$

poly-time [LPR10]

search ring-LWE

poly-time [LPR10]

decision ring-LWE

tight [ACPS09]

decision ring-LWE  
with short secrets

## Practice:

- Assume the best way to solve DRLWE is to solve LWE.
- Assume solving LWE involves a lattice reduction problem.
- Estimate parameters based on runtime of lattice reduction algorithms e.g. [APS15]
- (Ignore non-tightness.)  
[CKMS16]

[LPR10] Lyubashevsky, Piekert, Regev. *EUROCRYPT 2010*.

[ACPS15] Applebaum, Cash, Peikert, Sahai. *CRYPTO 2009*.

[CKMS16] Chatterjee, Kobitz, Menezes, Sarkar. ePrint 2016/360.



# Basic ring-LWE-DH key agreement (unauthenticated)

- Reformulation of Peikert's ring-LWE KEM (*PQCrypto 2014*)

public: "big"  $a$  in  $R_q = \mathbf{Z}_q[x]/(x^n+1)$

**Alice**

secret:

random "small"  $s, e$  in  $R_q$

**Bob**

secret:

random "small"  $s', e'$  in  $R_q$

$$b = a \cdot s + e$$

$$b' = a \cdot s' + e'$$

shared secret:

$$s \cdot b' = s \cdot (a \cdot s' \cdot e') \approx s \cdot a \cdot s'$$

shared secret:

$$b \cdot s' \approx s \cdot a \cdot s'$$

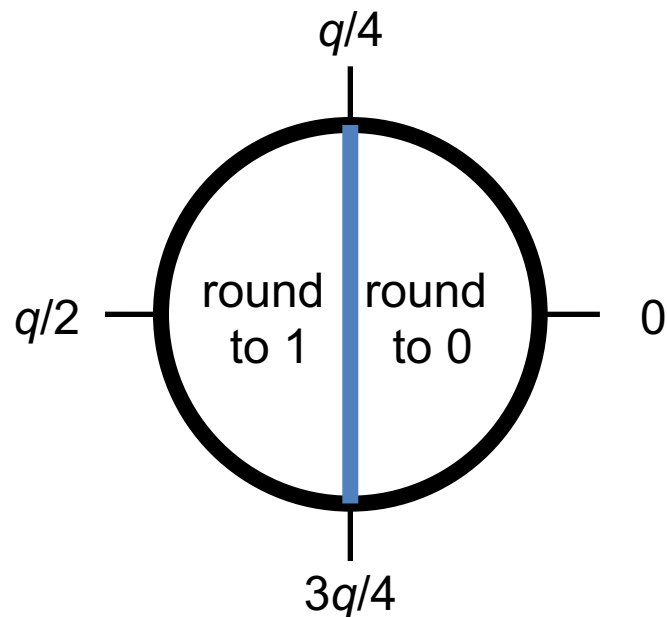
These are only approximately equal  $\Rightarrow$  need rounding

# Rounding

- Each coefficient of the polynomial is an integer modulo  $q$
- Treat each coefficient independently

# Basic rounding

- Round either to 0 or  $q/2$
- Treat  $q/2$  as 1

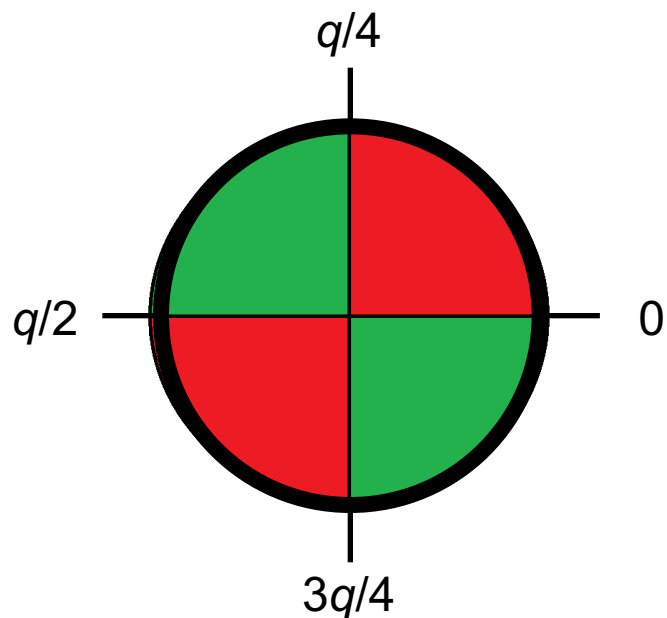


This works  
most of the time:  
prob. failure  $2^{-10}$ .

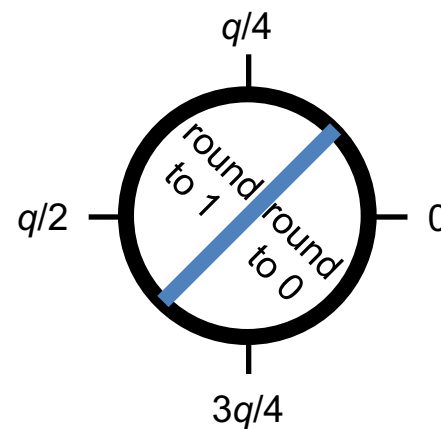
Not good enough:  
we need exact key  
agreement.

# Better rounding (Peikert)

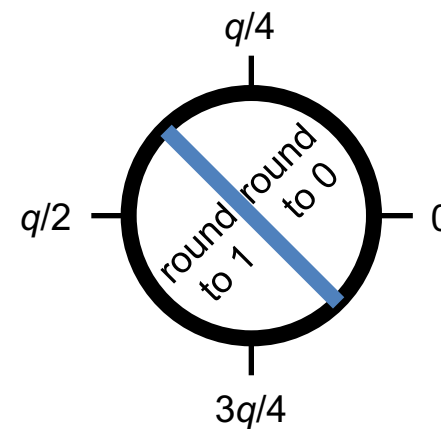
Bob says which of two regions the value is in:  or 



If

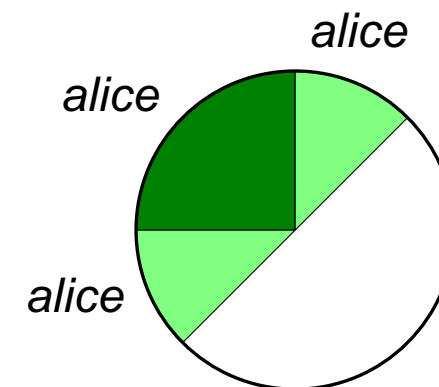
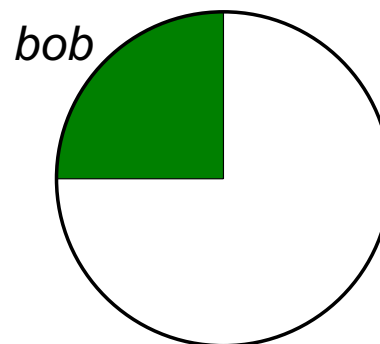
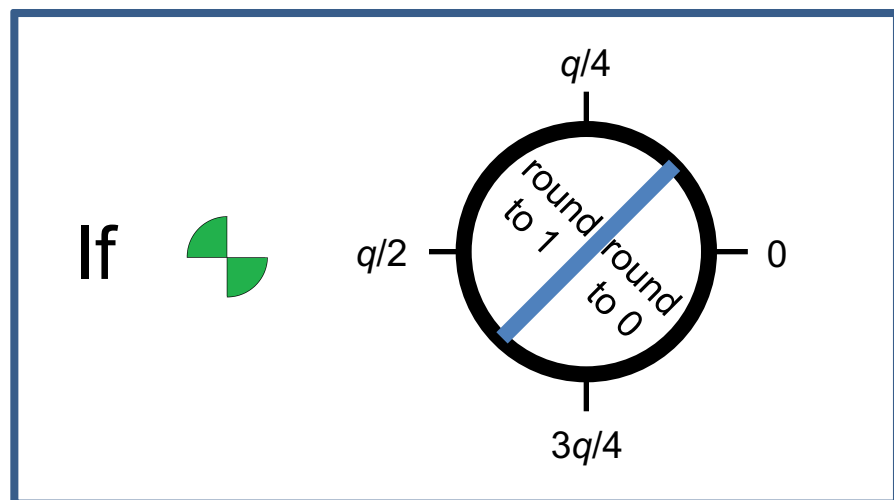




If



# Better rounding (Peikert)

- If  $| \text{alice} - \text{bob} | \leq q/8$ , then this always works.



- For our parameters, probability  $| \text{alice} - \text{bob} | > q/8$  is less than  $2^{-128000}$ .
- Security not affected: revealing  or  leaks no information

# Exact ring-LWE-DH key agreement (unauthenticated)

- Reformulation of Peikert's R-LWE KEM (*PQCrypto 2014*)

public: "big"  $a$  in  $R_q = \mathbf{Z}_q[x]/(x^n+1)$

**Alice**

secret:

random "small"  $s, e$  in  $R_q$

**Bob**

secret:

random "small"  $s', e'$  in  $R_q$

$$b = a \cdot s + e$$



$$b' = a \cdot s' + e', \quad \text{or}$$



shared secret:

$\text{round}(s \cdot b')$

shared secret:

$\text{round}(b \cdot s')$

# Ring-LWE-DH key agreement

---

## Public parameters

---

Decision R-LWE parameters  $q, n, \chi$

$$a \stackrel{\$}{\leftarrow} \mathcal{U}(R_q)$$

---

**Alice**

$$s, e \stackrel{\$}{\leftarrow} \chi$$

$$b \leftarrow as + e \in R_q$$

**Bob**

$$s', e' \stackrel{\$}{\leftarrow} \chi$$

$$b' \leftarrow as' + e' \in R_q$$

$$e'' \stackrel{\$}{\leftarrow} \chi$$

$$v \leftarrow bs' + e'' \in R_q$$

$$\bar{v} \stackrel{\$}{\leftarrow} \text{dbl}(v) \in R_{2q}$$

$$c \leftarrow \langle \bar{v} \rangle_{2q,2} \in \{0, 1\}^n$$

$$k_B \leftarrow \lfloor \bar{v} \rfloor_{2q,2} \in \{0, 1\}^n$$

$$k_A \leftarrow \text{rec}(\lfloor 2b's \rfloor c) \in \{0, 1\}^n$$

---

Secure if  
decision ring  
learning with  
errors problem is  
hard.

# Parameters

160-bit classical security,  
80-bit quantum security

- $n = 1024$
- $q = 2^{32} - 1$
- $\chi$  = discrete Gaussian with parameter  $\sigma = 8/\sqrt{2\pi}$
- Failure:  $2^{-12800}$
- Total communication: 8.1 KiB



Implementation aspect 1:

## Polynomial arithmetic

- Polynomial multiplication in  $R_q = \mathbf{Z}_q[x]/(x^{1024}+1)$  done with Nussbaumer's FFT:

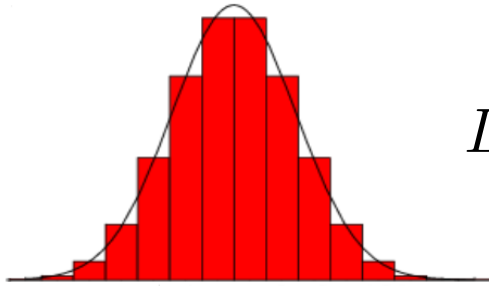
If  $2^m = rk$ , then

$$\frac{R[X]}{\langle X^{2^m} + 1 \rangle} \cong \frac{\left( \frac{R[Z]}{\langle Z^r + 1 \rangle} \right) [X]}{\langle X^k - Z \rangle}$$

- Rather than working modulo degree-1024 polynomial with coefficients in  $\mathbf{Z}_q$ , work modulo:
  - degree-256 polynomial whose coefficients are themselves polynomials modulo a degree-4 polynomial,
  - or degree-32 polynomials whose coefficients are polynomials modulo degree-8 polynomials whose coefficients are polynomials
  - or ...

Implementation aspect 2:

## Sampling discrete Gaussians



$$D_{\mathbb{Z},\sigma}(x) = \frac{1}{S} e^{-\frac{x^2}{2\sigma^2}} \quad \text{for } x \in \mathbb{Z}, \sigma \approx 3.2, S = 8$$

- Security proofs require “small” elements sampled within statistical distance  $2^{-128}$  of the true discrete Gaussian
- We use inversion sampling: precompute table of cumulative probabilities
  - For us: 52 elements, size = 10000 bits
- Sampling each coefficient requires six 192-bit integer comparisons and there are 1024 coefficients
  - $51 \cdot 1024$  for constant time

# Sampling is expensive

Operation	Cycles	
	constant-time	non-constant-time
sample $\stackrel{\$}{\leftarrow} \chi$	1 042 700	668 000
FFT multiplication	342 800	—
FFT addition	1 660	—
dbl( $\cdot$ ) and crossrounding $\langle \cdot \rangle_{2q,2}$	23 500	21 300
rounding $\lfloor \cdot \rfloor_{2q,2}$	5 500	3,700
reconciliation $\text{rec}(\cdot, \cdot)$	14 400	6 800

# “NewHope”

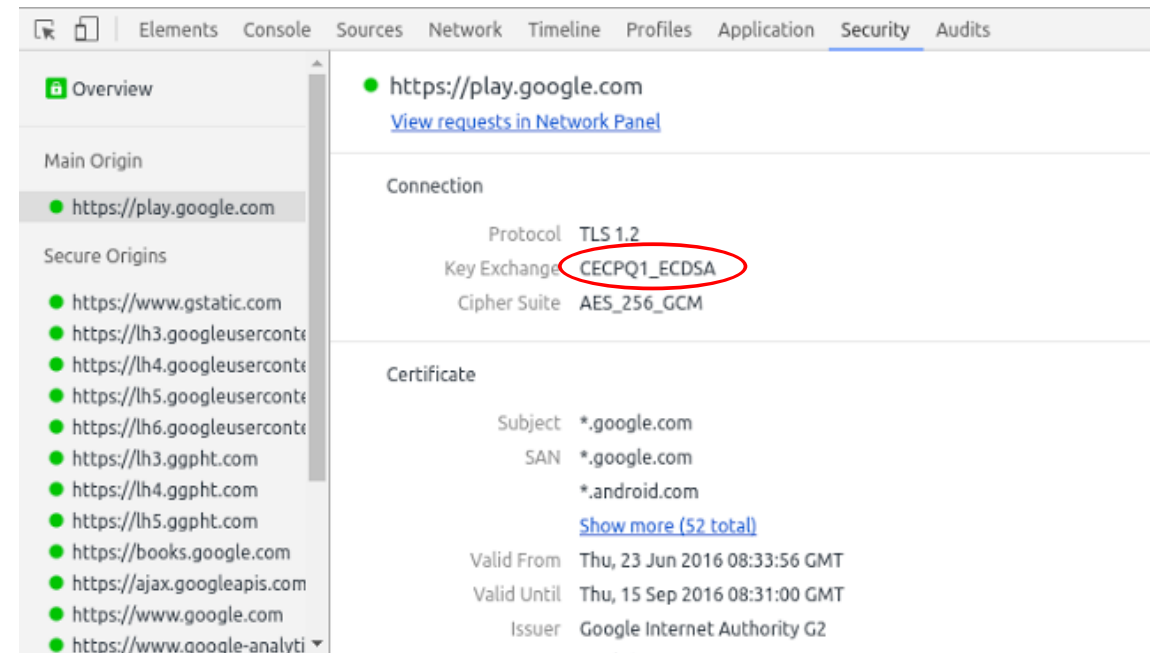
Alkim, Ducas, Pöppelman, Scwabe.  
*USENIX Security 2016*

- New parameters
- Different error distribution
- Improved performance
- Pseudorandomly generated parameters
- Further performance improvements by others [GS16, LN16, ...]

## Google Security Blog

### Experimenting with Post-Quantum Cryptography

July 7, 2016



The screenshot shows the Chrome DevTools Security tab for the URL <https://play.google.com>. The connection details are as follows:

Property	Value
Protocol	TLS 1.2
Key Exchange	CECPQ1_ECDSA
Cipher Suite	AES_256_GCM

The Certificate details are:

Property	Value
Subject	*.google.com
SAN	*.google.com *.android.com
Valid From	Thu, 23 Jun 2016 08:33:56 GMT
Valid Until	Thu, 15 Sep 2016 08:31:00 GMT
Issuer	Google Internet Authority G2

# Key agreement from LWE

---

Bos, Costello, Ducas, Mironov, Naehrig, Nikolaenko, Raghunathan, Stebila.  
Frodo: Take off the ring! Practical, quantum-safe key exchange from LWE.  
*ACM Conference on Computer and Communications Security (CCS) 2016.*

<https://eprint.iacr.org/2016/659>

## Decision learning with errors problem with short secrets

**Definition.** Let  $n, q \in \mathbb{N}$ . Let  $\chi$  be a distribution over  $\mathbb{Z}$ .

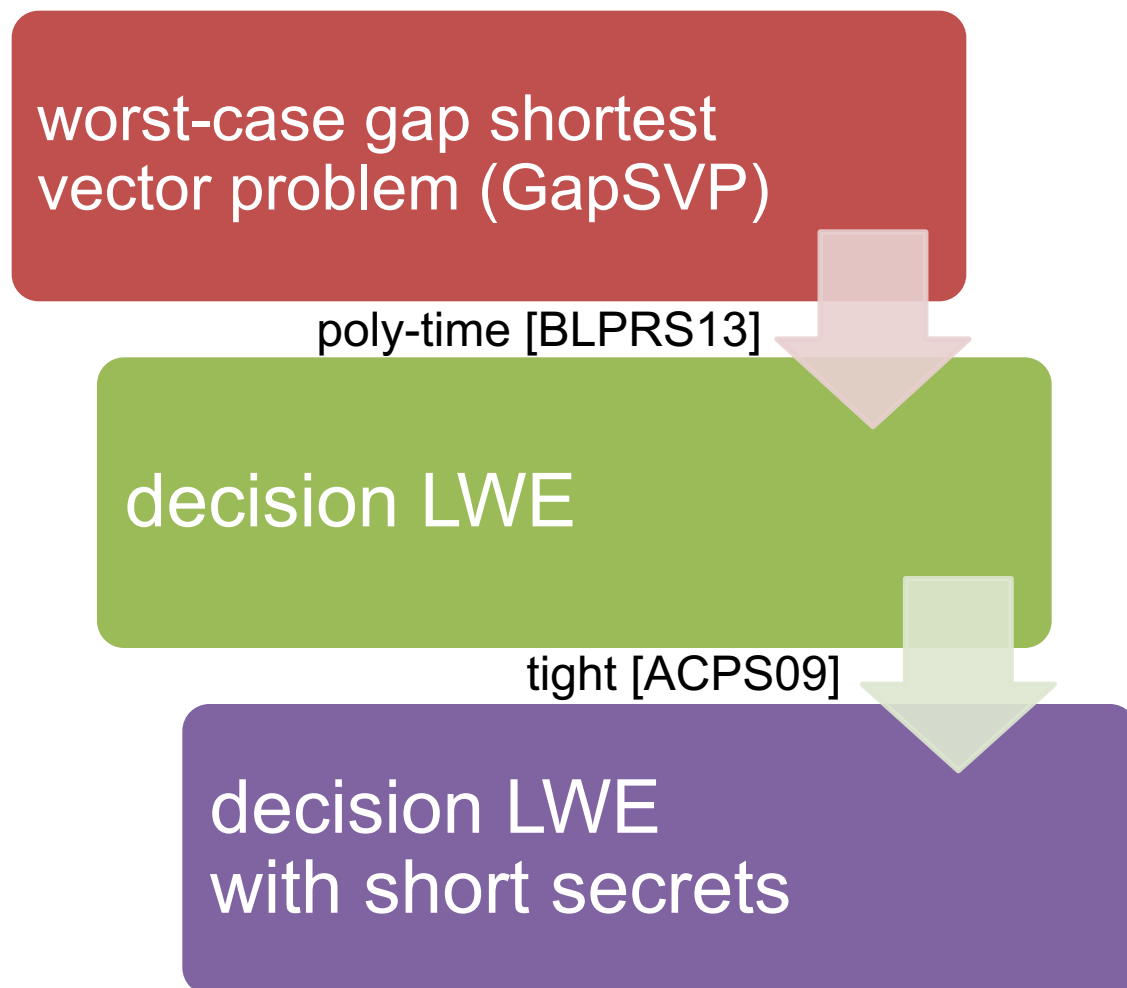
Let  $\mathbf{s} \stackrel{\$}{\leftarrow} \chi^n$ .

Define:

- $O_{\chi, \mathbf{s}}$ : Sample  $\mathbf{a} \stackrel{\$}{\leftarrow} \mathcal{U}(\mathbb{Z}_q^n)$ ,  $e \stackrel{\$}{\leftarrow} \chi$ ; return  $(\mathbf{a}, \mathbf{a} \cdot \mathbf{s} + e)$ .
- $U$ : Sample  $(\mathbf{a}, b') \stackrel{\$}{\leftarrow} \mathcal{U}(\mathbb{Z}_q^n \times \mathbb{Z}_q)$ ; return  $(\mathbf{a}, b')$ .

The *decision LWE problem with short secrets* for  $n, q, \chi$  is to distinguish  $O_{\chi, \mathbf{s}}$  from  $U$ .

# Hardness of decision LWE



## Practice:

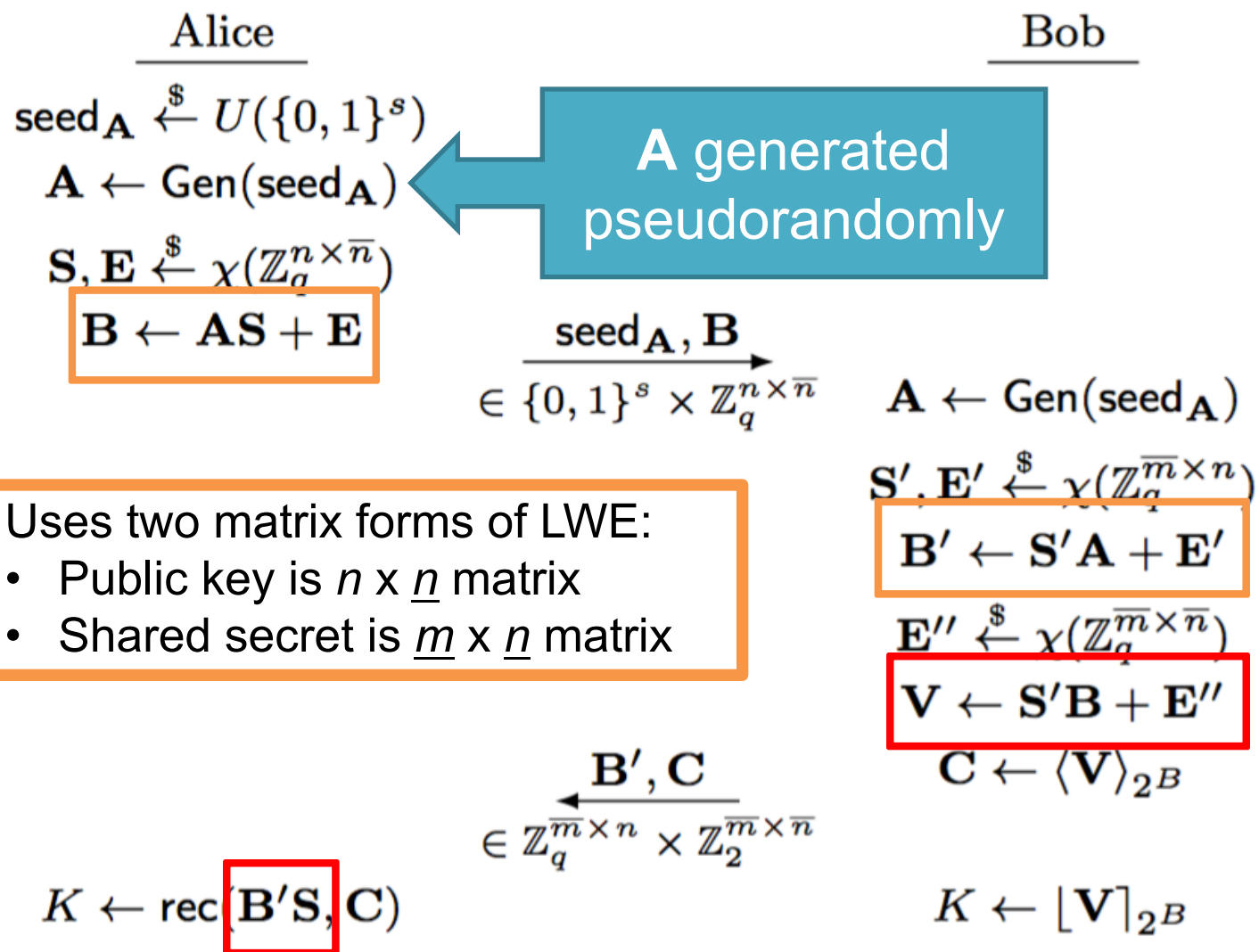
- Assume the best way to solve DLWE is to solve LWE.
- Assume solving LWE involves a lattice reduction problem.
- Estimate parameters based on runtime of lattice reduction algorithms.
- (Ignore non-tightness.)

# Generic vs. ideal lattices

- Ring-LWE matrices have additional structure
  - Relies on hardness of a problem in **ideal** lattices
- LWE matrices have no additional structure
  - Relies on hardness of a problem in **generic** lattices
- NTRU also relies on a problem in a type of ideal lattices
- Currently, best algorithms for ideal lattice problems are essentially the same as for generic lattices
  - Small constant factor improvement in some cases
- If we want to eliminate this additional structure, can we still get an efficient algorithm?



# “Frodo”: LWE-DH key agreement



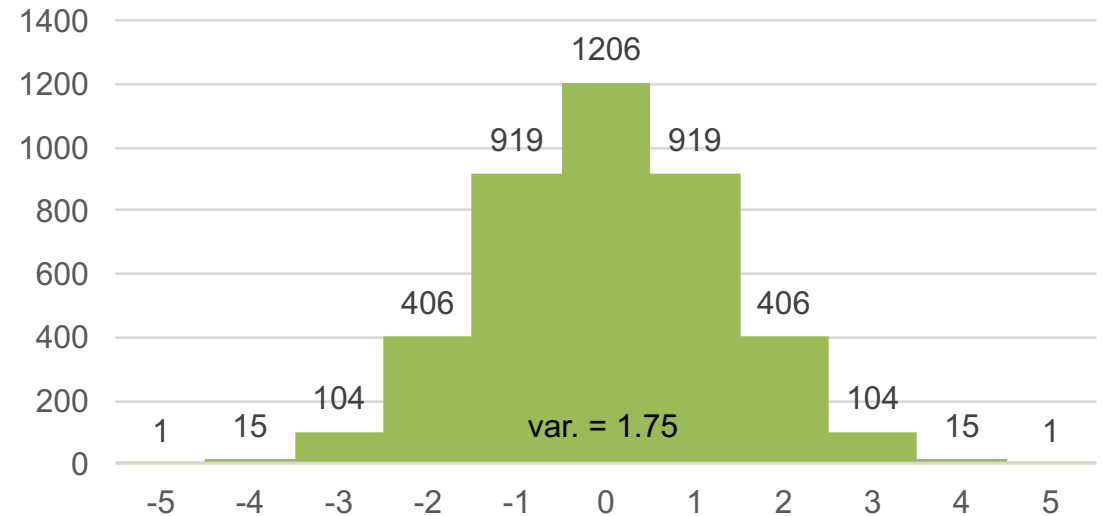
Secure if decision learning with errors problem is hard (and Gen is a secure PRF).

# Rounding

- We extract 4 bits from each of the 64 matrix entries in the shared secret.
  - More granular form of Peikert's rounding.

Parameter sizes, rounding, and error distribution all found via search scripts.

# Error distribution



- Close to discrete Gaussian in terms of Rényi divergence (1.000301)
- Only requires 12 bits of randomness to sample

# Parameters

All known variants of the sieving algorithm require a list of vectors to be created of this size

## “Recommended”

- 156-bit classical security, 142-bit quantum security, 112-bit plausible lower bound
- $n = 752, m = 8, q = 2^{15}$
- $\chi$  = approximation to rounded Gaussian with 11 elements
- Failure:  $2^{-36.5}$
- Total communication: 22.6 KiB

## “Paranoid”

- 191-bit classical security, 174-bit quantum security, 138-bit plausible lower bound
- $n = 864, m = 8, q = 2^{15}$
- $\chi$  = approximation to rounded Gaussian with 13 elements
- Failure:  $2^{-35.8}$
- Total communication: 25.9 KiB

# Standalone performance

---

# Implementations

## Our implementations

- BCNS15
- Frodo

Pure C implementations

Constant time

## Compare with others

- RSA 3072-bit (OpenSSL 1.0.1f)
- ECDH nistp256 (OpenSSL)

Use assembly code

- NewHope
- NTRU EES743EP1
- SIDH (Isogenies) (MSR)

Pure C implementations

# Standalone performance

Scheme	Alice0	Bob	Alice1	Communication (bytes)		Claimed security	
	(ms)	(ms)	(ms)	A→B	B→A	classical	quantum
RSA 3072-bit	—	0.09	4.49	387 / 0*	384	128	—
ECDH nistp256	0.366	0.698	0.331	32	32	128	—
BCNS	1.01	1.59	0.174	4,096	4,224	163	76
NewHope	0.112	0.164	0.034	1,824	2,048	229	206
NTRU EES743EP1	2.00	0.281	0.148	1,027	1,022	256	128
SIDH	135	464	301	564	564	192	128
<b>Frodo Recomm.</b>	<b>1.13</b>	<b>1.34</b>	<b>0.13</b>	<b>11,377</b>	<b>11,296</b>	<b>156</b>	<b>142</b>
Frodo Paranoid	1.25	1.64	0.15	13,057	12,976	191	174

# Standalone performance

RSA 3072-bit	Fast (4 ms)	Small (0.3 KiB)
ECDH <i>nistp256</i>	Very fast (0.7 ms)	Very small (0.03 KiB)
BCNS	Fast (1.5 ms)	Medium (4 KiB)
NewHope	Very fast (0.2 ms)	Medium (2 KiB)
NTRU <i>EES743EP1</i>	Fast (0.3–1.2 ms)	Medium (1 KiB)
SIDH	Very slow (400 ms)	Small (0.5 KiB)
Frodo Recommended	Fast (1.4 ms)	Large (11 KiB)
McBits*	Very fast (0.5 ms)	Very large (360 KiB)

\* McBits results from source paper [BCS13] Bernstein, Chou, Schwabe. *CHES 2013*.

Note somewhat incomparable security levels

# TLS integration and performance

---

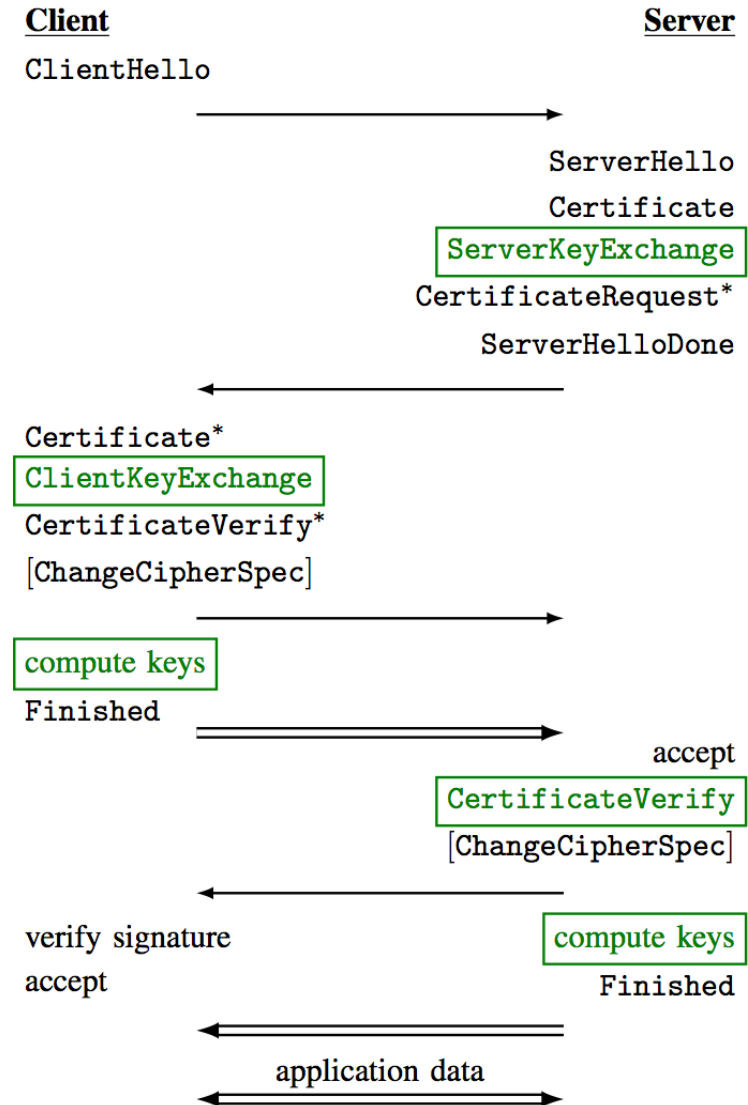


# Integration into TLS 1.2

## New ciphersuite:

**TLS-KEX-SIG-AES256-GCM-SHA384**

- SIG = RSA or ECDSA signatures for authentication
- KEX = Post-quantum key exchange
- AES-256 in GCM for authenticated encryption
- SHA-384 for HMAC-KDF



# Security within TLS 1.2

## Model:

- authenticated and confidential channel establishment (ACCE) [JKSS12]

## Theorem:

- signed LWE/ring-LWE ciphersuite is ACCE-secure if underlying primitives (signatures, LWE/ring-LWE, authenticated encryption) are secure
  - Interesting technical detail for ACCE provable security people: need to move server's signature to end of TLS handshake because oracle-DH assumptions don't hold for ring-LWE or use an IND-CCA KEM for key exchange via e.g. [FO99]

# TLS performance

## Handshake latency

- Time from when client sends first TCP packet till client receives first application data
- No load on server

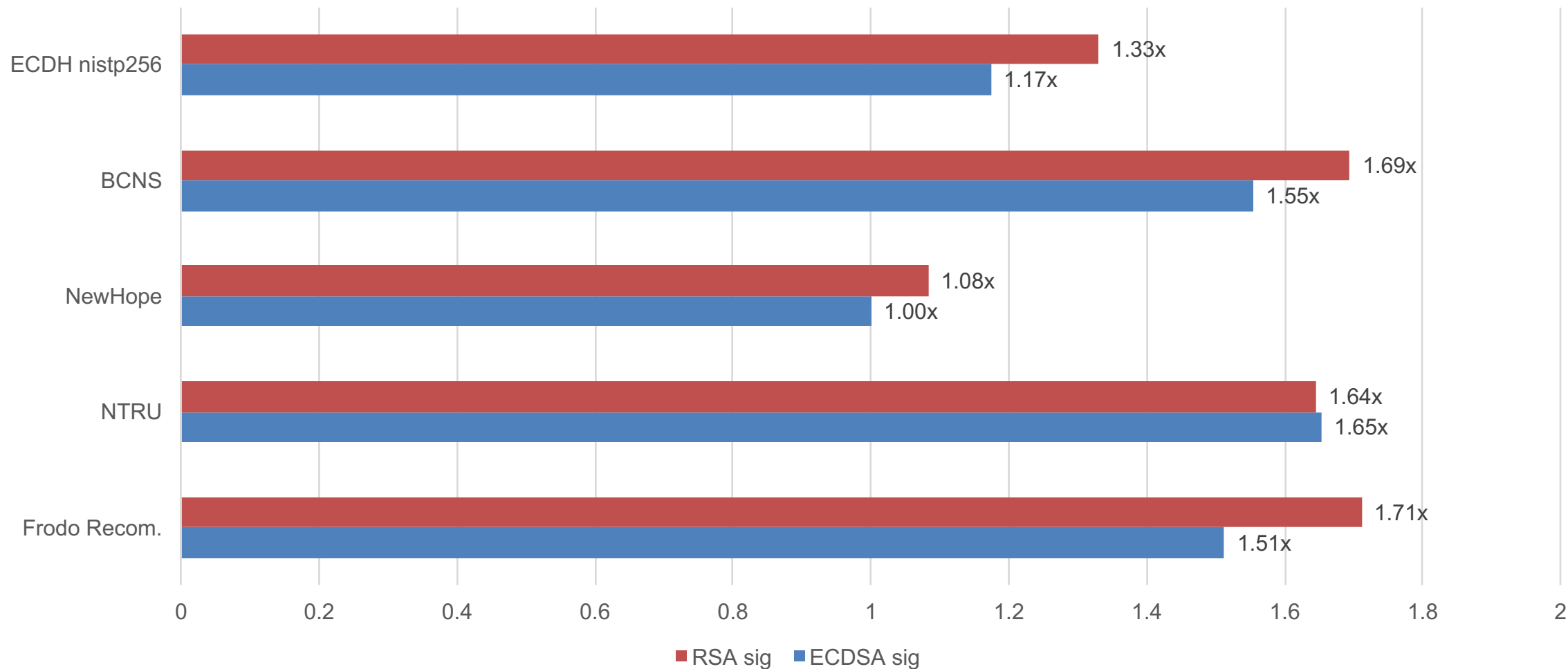
## Connection throughput

- Number of connections per second at server before server latency spikes

# TLS handshake latency

compared to NewHope-ECDSA

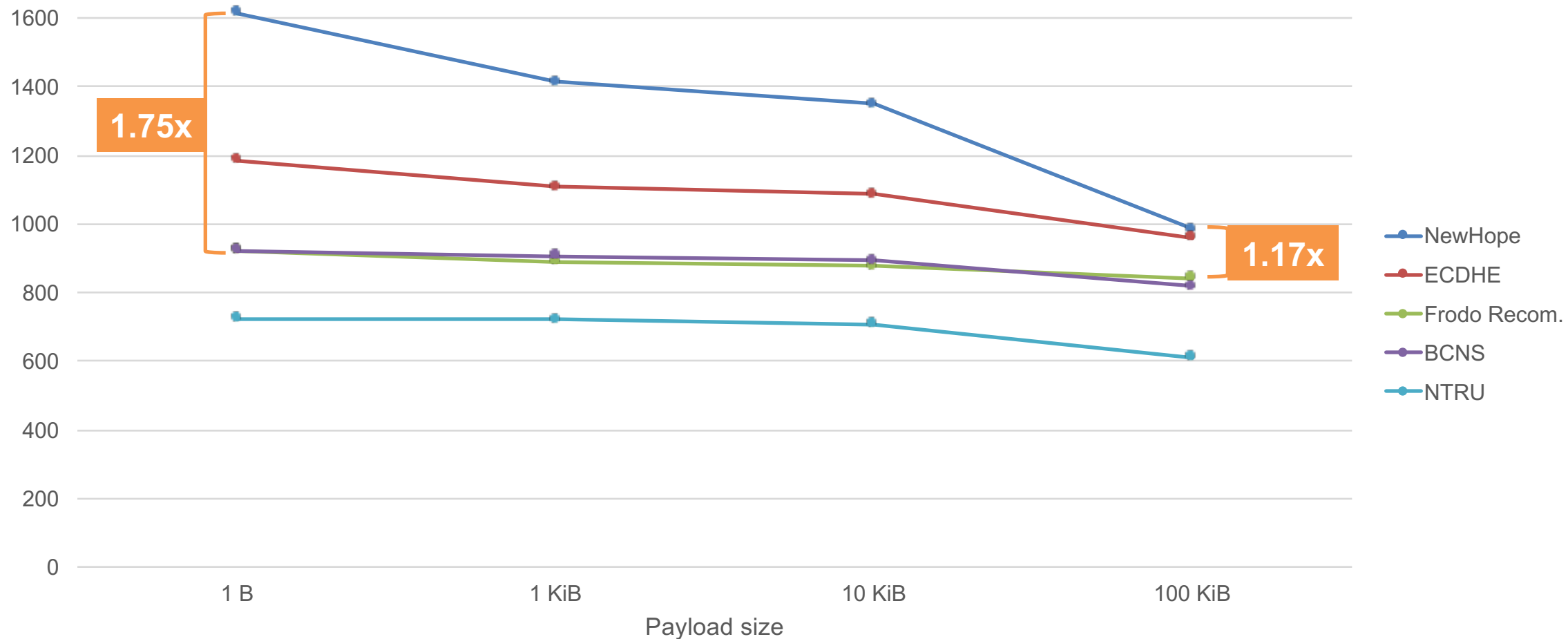
smaller (left) is better



# TLS connection throughput

ECDSA signatures

bigger (top) is better



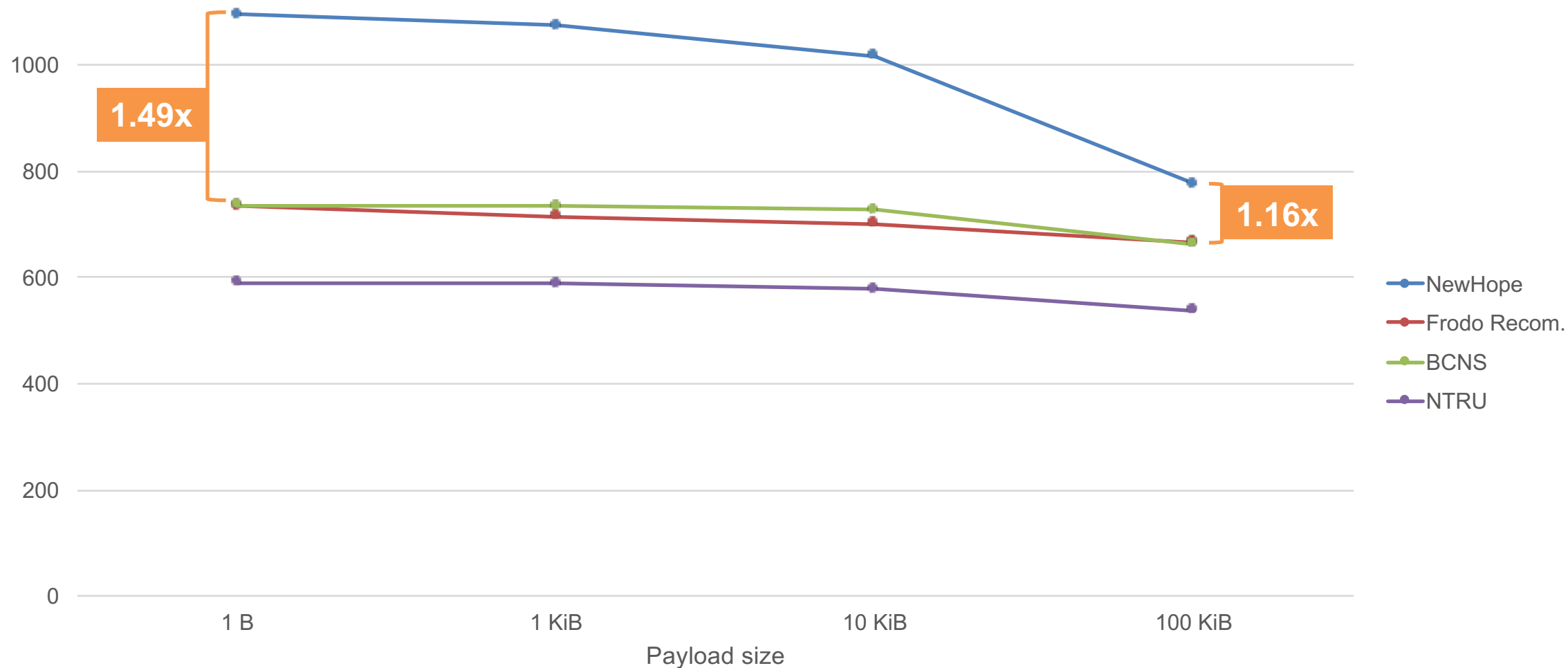
# Hybrid ciphersuites

- Use both post-quantum key exchange and traditional key exchange
- Example:
  - ECDHE + NewHope
    - Used in Google Chrome experiment
  - ECDHE + Frodo
- Session key secure if either problem is hard
- Why use post-quantum?
  - (Potential) security against future quantum computer
- Why use ECDHE?
  - Security not lost against existing adversaries if post-quantum cryptanalysis advances

# TLS connection throughput – hybrid w/ECDHE

ECDSA signatures

bigger (top) is better



# Open Quantum Safe

---

Collaboration with Mosca et al., University of Waterloo

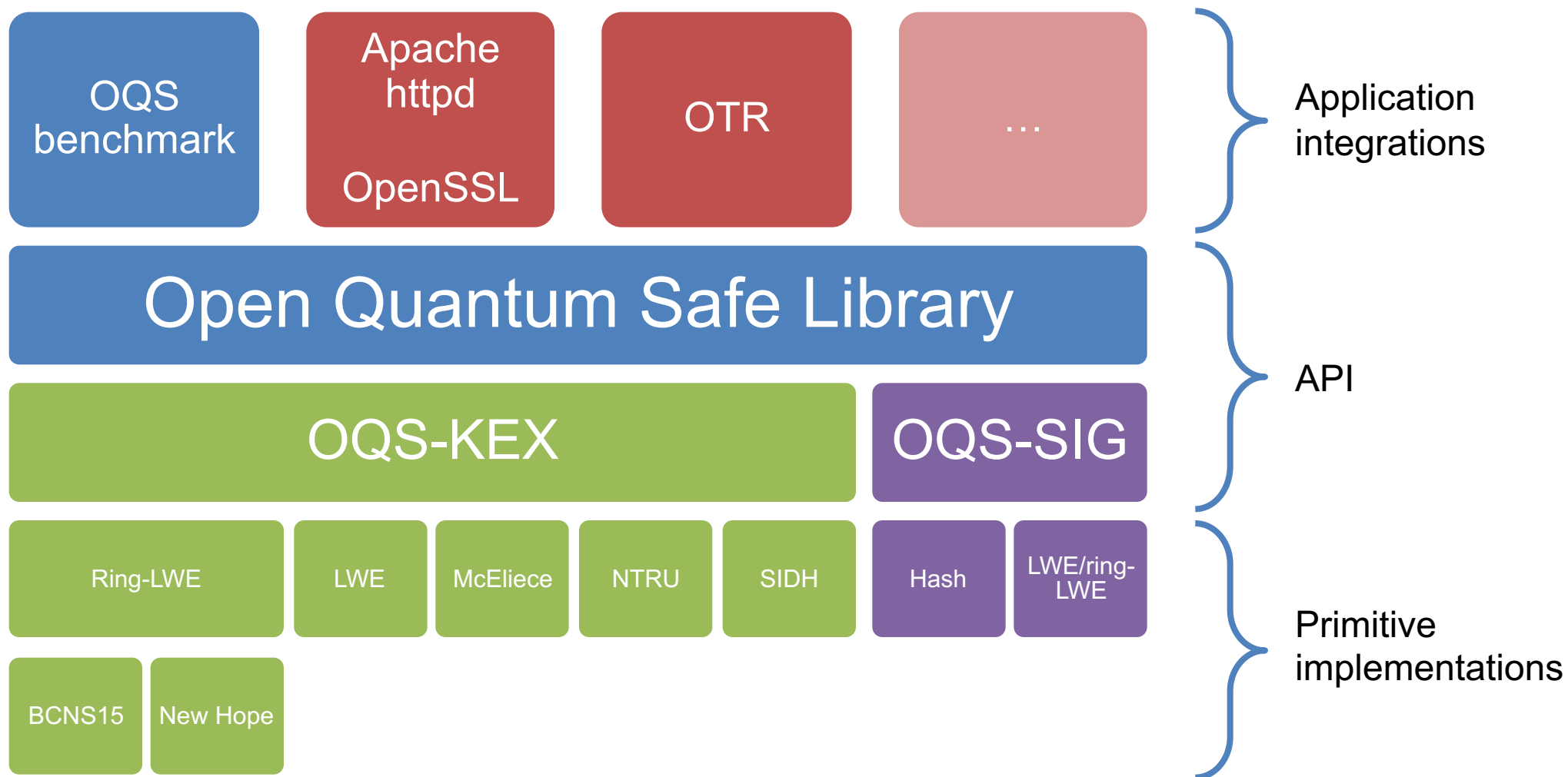
<https://github.com/open-quantum-safe/>



# Open Quantum Safe

- Open source C library
  - Common interface for key exchange and digital signatures
1. Collect post-quantum implementations together
    - Our own software
    - Thin wrappers around existing open source implementations
    - Contributions from others
  2. Enable direct comparison of implementations
  3. Support prototype integration into application level protocols
    - Don't need to re-do integration for each new primitive – how we did Frodo experiments

# Open Quantum Safe architecture



# Getting involved and using OQS

<https://github.com/open-quantum-safe/>

If you're writing post-quantum implementations:

- We'd love to coordinate on API
- And include your software if you agree

If you want to prototype or evaluate post-quantum algorithms in applications:

- Maybe OQS will be helpful to you

We'd love help with:

- Code review and static analysis
- Signature scheme implementations
- Additional application-level integrations

# Summary

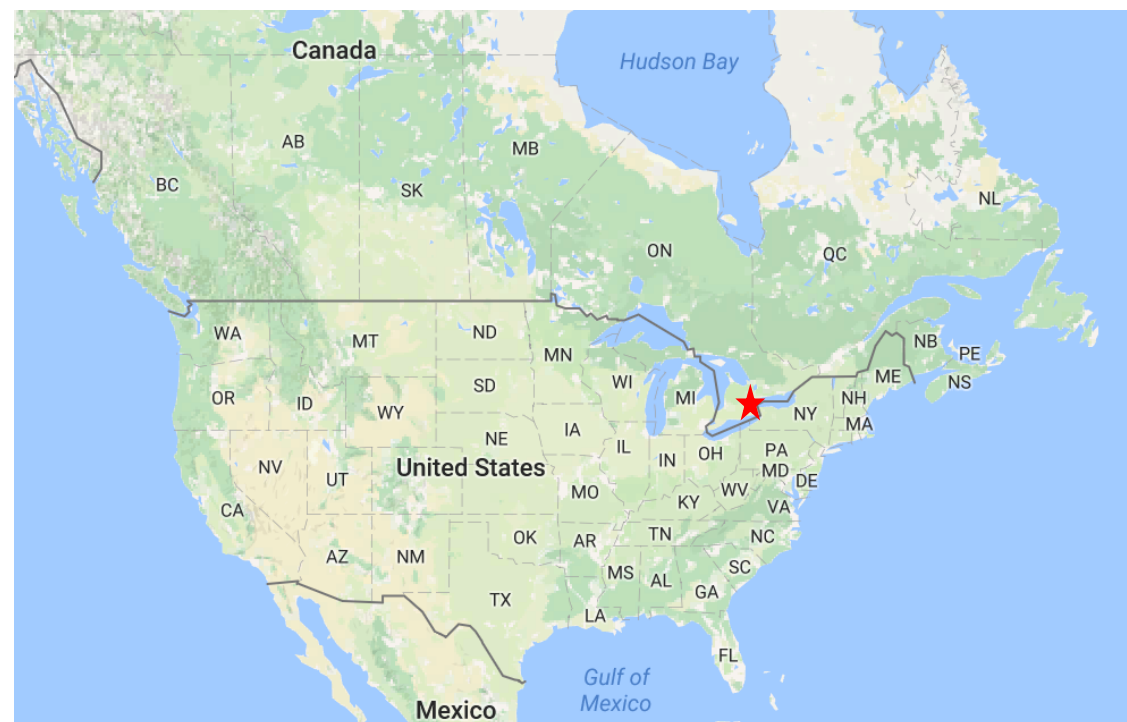
---

# Summary

- Exciting research area – lots of opportunities!
- Ring-LWE is fast and fairly small
- LWE can achieve reasonable key sizes
- Hybrid ciphersuites will probably play a role in the transition
- Performance differences are muted in application-level protocols
- Parameter sizes and efficiency likely to evolve
- Post-quantum key exchange soon to be in demand

# Now hiring!

- Post-doc in any area of post-quantum cryptography
  - Applied or theoretical
- Deadline: August 25, 2016



For more info:

<https://www.douglas.stebila.ca/research/postdoc/>

# Links

## Ring-LWE key exchange

- <https://eprint.iacr.org/2014/599>
- <https://github.com/dstebila/rlwekex>

## LWE key exchange (Frodo)

- <https://eprint.iacr.org/2016/659>
- <https://github.com/lwe-frodo/>  
(coming soon)

## Open Quantum Safe

- <https://github.com/open-quantum-safe/>

## Post-doc

- <https://www.douglas.stebila.ca/research/postdoc/>