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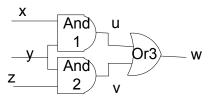
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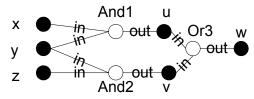
# **Applications of graphs**

## **Topological Structure of Circuit**

A circuit consists of components and nets.



We can model components and nets as vertices. Edges are labeled with names of "ports"



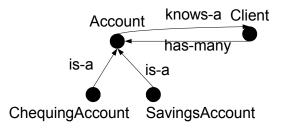
## **Topological structure of software**

Components are classes.

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#### Edges represent relationships between classes.



### Structured text

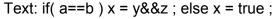
A graph that is connected and has no cycles is called a tree.

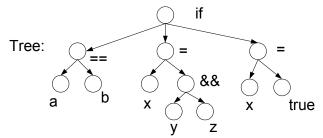
Text documents often encode an underlying tree structure.

Examples include HTML, XML, and programming languages.

2

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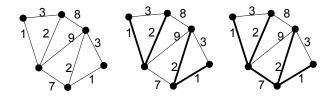




# Weighted graphs and minimal spanning trees

Suppose you need to put power lines (or fibre optic cable) on a island. The source and each house needs to be connected. There are a number of possible routes based on existing infrastructure, each with an associated positive cost. We need the minimal-weight connected sub-graph that includes every vertex.

An undirected graph that is connected and has no cycles is called an **undirected tree**. Thus we need a *minimal spanning tree* 



**Algorithm** (Kruskal): Start with T an empty graph. Consider the edges in order of increasing weight. Add an edge to T if it does not create a cycle

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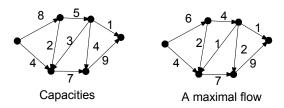
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# Weighted graphs and max flow

Consider a power network consisting of 1 generating station (**source**), 1 destination station (**sink**), any number of intermediate stations, distribution lines each labelled with a capacity.

We model with a weighted directed graph:



A **flow** is a labelling of the edges such that.

- No edge exceeds its capacity
- Each nonsink/nonsource vertex has equal in-flow and out-flow.

The *maximum flow problem* is to find a flow that maximized the flow into the sink.

A **cut** is a set of edges, the removal of which, disconnects the source from the sink.

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**Theorem** (Ford & Fulkerson): The value of the maximal flow equals the minimum capacity of any cut.

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