## ENGI 4421

Term Test 1
2020 June 11

1. A random sample of 100 contractors for a certain type of design project returns the following summary data and histogram for completion times ( $t$, in days).

| Variable | N | Mean | StDev | Minimum | Q1 | Median | Q3 | Maximum |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Completion time | 100 | 80.07 | 8.50 | 51 | 75 | 80 | 86 | 97 |

Histogram of Project Completion Time

(a) Find the modal class
[2]
(b) Find the frequency of the class $60 \leq t<70$ (days)
(c) Is the minimum value of 51 days an extreme outlier, a mild outlier, or not an outlier at all? Show your working.
2. Given the information for the three events $A, B, C$

$$
\begin{aligned}
& \mathrm{P}[A]=.50, \quad \mathrm{P}[B]=.46, \quad \mathrm{P}[C]=.40, \quad \mathrm{P}[A \cup B]=.59, \\
& \mathrm{P}[B \cup C]=.56, \quad \mathrm{P}[C \cup A]=.57, \quad \mathrm{P}[A \cup B \cup C]=.61
\end{aligned}
$$

(a) Find the probability that none of the events $A, B, C$ occur.
(b) Find the probability that exactly one of the events $A, B, C$ occurs.
(c) Find the exact value of $\mathrm{P}[B \mid C]$
(d) Convert your answer to part (c) into odds.
3. A board of directors must elect from among its twelve (12) members a chair, a vice chair, a secretary and a treasurer. No one director may be elected to more than one of these four offices.
(a) In how many distinct ways may these four officers be chosen?
(b) These four officers are the only members of the executive committee.

In how many distinct ways may the membership of the executive committee be chosen?

Show your working and express your final answers as single numbers.

## 4. BONUS QUESTION

Pumping stations A, B are connected in parallel to transport water from point X to point Y, as illustrated.


Each station works $80 \%$ of the time when the other station is working, but only $30 \%$ of the time when the other station has failed.

Find the probability that this system will transport water from point X to point Y .

