

General: All Coefficients Positive

$$a S^3 + b S^2 + c S + d = 0$$

$$x = bc - ad$$

$$a S^4 + b S^3 + c S^2 + d S + e = 0$$

$$x = bc - ad \quad y = dx - b^2e$$

$$a S^5 + b S^4 + c S^3 + d S^2 + e S + f = 0$$

$$x = bc - ad \quad y = be - af \quad z = (dx - by)y - x^2f$$

$$K_P = 0.6 * \mathbf{K_P} \quad K_I = K_P / T_I \quad K_D = K_P * T_D$$

$$T_I = 0.5 * \mathbf{T_P} \quad T_D = 0.125 * \mathbf{T_P}$$

$$\begin{aligned} & A e^{+at} + B e^{+bt} + N + M t \\ & + (X+Yj) e^{+(x+yj)t} + (X-Yj) e^{+(x-yj)t} \\ & + (G+Hj) e^{+\omega j t} + (G-Hj) e^{-\omega j t} \end{aligned}$$

$$\begin{aligned} & A e^{+at} + B e^{+bt} + N + M t \\ & + 2X e^{+xt} \text{Cos}[yt] - 2Y e^{+xt} \text{Sin}[yt] \\ & + 2G \text{Cos}[\omega t] - 2H \text{Sin}[\omega t] \end{aligned}$$

$$R=R_{\circ}+\Delta R\,\sin\,[\omega t]\qquad\qquad C=C_{\circ}\qquad\qquad D=D_{\circ}$$

$$Q \quad = \quad K_P \; E \quad + \quad K_I \; \int E d\tau \quad + \quad K_D \; dE/dt$$

$$Q \quad = \quad (\; K_P \; + \; K_I/S \; + \; K_DS \;) \; E$$

$$Q \quad = \quad (\; K_P \; + \; K_I \; TZ/[Z-1] \; + \; K_D \; [Z-1]/TZ \;) \; E$$

$$dG/dt = H \qquad \qquad G_{\mathrm{NEW}} = G_{\mathrm{OLD}} + \Delta t \; \star \; H_{\mathrm{OLD}}$$

$$O/I \, = \, G/(1+GH) \, = \, \mathbf{N/D} \qquad 1+GH \, = \, 1+N/D \, = \, (N+D)/D$$

$$1 \, + \, GH \, \, = \, \, \frac{K \, (S\!-\!Z_1) \, (S\!-\!Z_2) \, ::::: (S\!-\!Z_n)}{(S\!-\!P_1) \, (S\!-\!P_2) \, ::::: (S\!-\!P_m)}$$

$$= \; K \; [\Pi r_Z \angle \Sigma \theta_Z] \; / \; [\Pi r_P \angle \Sigma \theta_P] \; = \; R \angle \Theta$$

$$N=N_Z-N_P\qquad\qquad N_Z=N+N_P$$

$$\mathbf{D} = N+D \qquad \Sigma \Gamma/(S-\lambda) \qquad \Sigma \Gamma e^{+\lambda t}$$

$$A S^2 + B S + C = 0$$

$$\frac{[-B - \sqrt{B^2 - 4AC}]}{[2A]} \quad \frac{[-B + \sqrt{B^2 - 4AC}]}{[2A]}$$

$$F(S) = \mathfrak{F}[f(t)] = \int_0^{\infty} f(t) e^{-st} dt$$

$$\mathfrak{F}[df/dt] = S F(S) \quad \mathfrak{F} \int f d\tau = F(S) / S$$

$$\mathfrak{F}[d^2f/dt^2] = S^2 F(S) \quad \mathfrak{F}[d^3f/dt^3] = S^3 F(S)$$

$$\mathfrak{F}(\text{Step with Height } A) = A/S$$

$$\mathfrak{F}(\text{Short Duration Pulse}) = AT$$

$$\mathfrak{F}(\text{Sine Wave}) = A\omega / (S^2 + \omega^2)$$

$$\mathfrak{F}(\text{Cosine Wave}) = AS / (S^2 + \omega^2)$$

$$\mathfrak{F}(\text{Linear Ramp}) = A/S^2$$

$$\mathfrak{F}(f[t-T]) = e^{-sT} F(S)$$

$$\lim_{t \rightarrow \infty} f(t) = \lim_{S \rightarrow 0} S F(S)$$

$$z = x + y j \quad z = r\angle\theta = re^{j\theta}$$

$$e^{+j\theta} = \cos\theta + j \sin\theta \quad e^{-j\theta} = \cos\theta - j \sin\theta$$

$$\sin\theta = (e^{+j\theta} - e^{-j\theta}) / 2j \quad \cos\theta = (e^{+j\theta} + e^{-j\theta}) / 2$$

$$y(t) = \sum_{n=0}^N x(n\Delta\tau)\Delta\tau \; h(t-n\Delta\tau)$$

$$y(t) = \int\limits_0^t x(\tau) \; h(t-\tau) \; d\tau$$

$$Y(S) = X(S) \; \mathbf{H}(S) = X(S) \; TF(S)$$

$$1 + GH = 0 \qquad GH = -1$$

$$\text{Magnitude } 1 \qquad \text{Angle } 180$$

$$\frac{M}{N \; (S-a) \; (S-b) \; (S-c)}$$

$$h^*(t) = \sum h(nT) \; \delta(t-nT)$$

$$H(Z) = \sum h(nT) \; Z^{-n} \qquad Z = e^{sT}$$

$$h(t) = \sum \Gamma \; e^{\lambda t} \qquad H(S) = \sum \Gamma / (S-\lambda)$$

$$H(Z) = \sum \Gamma / (1 - e^{\lambda T} \; Z^{-1}) \qquad Z = e^{\lambda T}$$

$$DF = [4Q_o]/[\pi E_o]$$

$$DF = 0 \qquad E_o < B$$

$$DF = [4Q_o]/[\pi E_o] \sqrt{[1-(B/E_o)^2]} \qquad E_o > B$$

$$B \sqrt{2} \qquad [2Q_o]/[\pi B]$$

$$[2Q_o]/[\pi K] \qquad [2Q_o]/[\pi K] \sqrt{2}$$

$$DF = K \qquad E_o < B$$

$$DF = [2K]/[\pi] [\theta + B/E_o \cos(\theta)] \qquad E_o > B$$

$$\theta = \sin^{-1} [B/E_o]$$

$$DF = 0 \qquad E_o < B$$

$$DF = K [1 - [2/\pi] [\theta + B/E_o \cos(\theta)]] \qquad E_o > B$$

$$\theta = \sin^{-1} [B/E_o]$$

$$DF = K + [4Q_o]/[\pi E_o]$$

$$DF = [4Q_o]/[\pi E_o] \quad j \qquad E_o < B$$

$$DF = M + N \quad j \qquad E_o > B$$

$$M = [4Q_o]/[\pi E_o] \sqrt{[1-(B/E_o)^2]}$$

$$N = [4Q_o]/[\pi E_o] (B/E_o)$$

```
num=[a b :]      den=[i j k :]
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```
sys=tf(num den)      impulse(sys)
```

```
step(sys)      num=[n m :]      den=[u v w :]
```

```
[r,p,k]=residue(num den)      state=ss(tf)
```

```
q=[A B C D E :]      p=roots(q)      plot(x,y)
```

```
dx/dt = A x + B u      y = C x + D u
```

```
dg=c2d(g # 'zoh')      z=tf('z' #)      dh=1/z
```

```
s=complex(0.0 w)      gh=num/den
```

```
num=as+b      den=xs2+ys=z
```

```
real(gh)      imag(gh)
```

```
rlocus(gh)      nyquist(gh)      bode(gh)
```

```
series(A B)      feedback(G H)
```

```
for a=1:b      ??????      end
```

```
if(?????)      ??????      end
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