

## APPLICATION: IDEAL ROCKET NOZZLE

Flow through an ideal rocket nozzle is everywhere isentropic. Gas comes out of the nozzle with a pressure that matches that of the surroundings. The combustion chamber is taken to be large. Let  $U$  denote the combustion chamber,  $D$  denote the nozzle exit and  $T$  denote the throat. The Mach Number in the combustion chamber is approximately zero and the Mach Number at the throat is unity. The thrust generated by the nozzle is

$$\bullet \dot{M} U_D$$

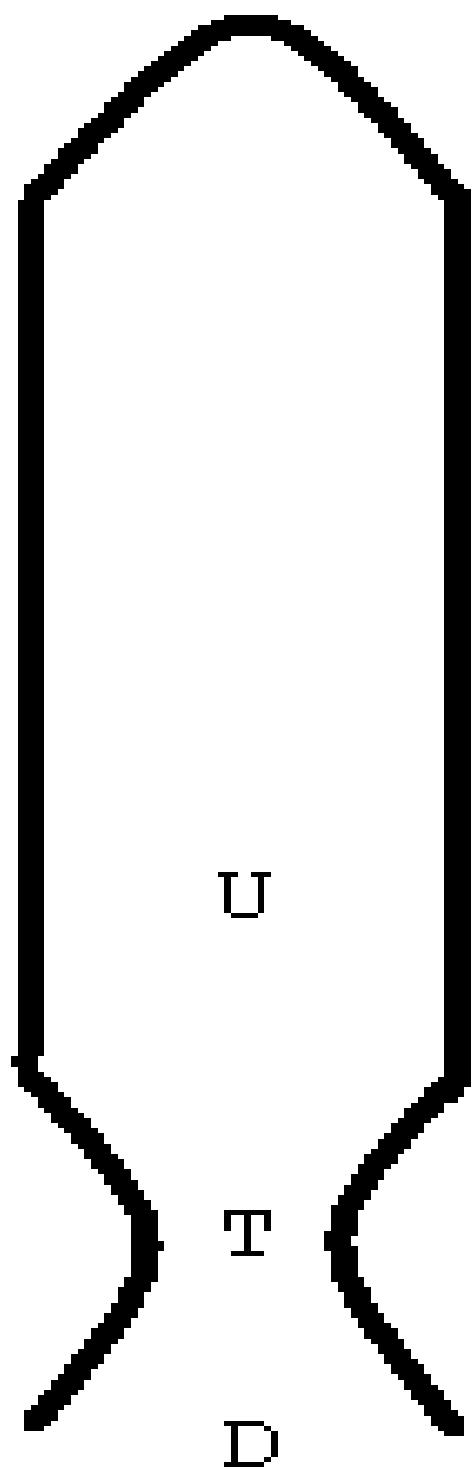
The mass flow rate anywhere in the nozzle is

$$\bullet \dot{M} = \rho A U$$

With known pressure and temperature in the combustion chamber, the isentropic ratios can be used to get pressure and temperature at the throat. One can then write

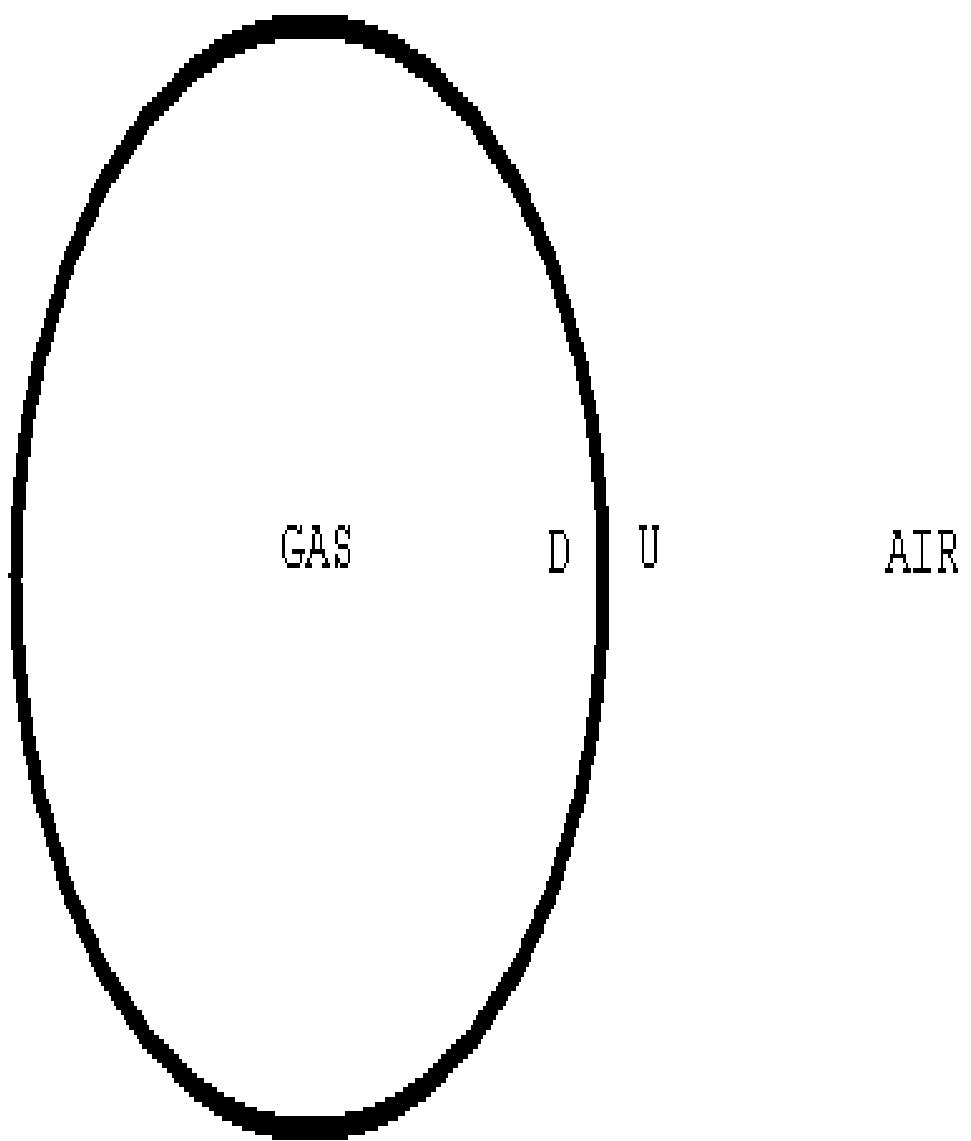
$$\bullet \dot{M} = P_T / [R T_T] A_T \sqrt{k R T_T}$$

With the combustion chamber and nozzle exit pressures known, the pressure ratio equation gives the Mach Number  $M_D$  at the exit. The temperature ratio equation then gives the temperature  $T_D$  at the exit. This allows us to calculate the sound speed  $C_D$  at the exit. With known Mach Number and sound speed, one can calculate the gas speed  $U_D$  at the exit.



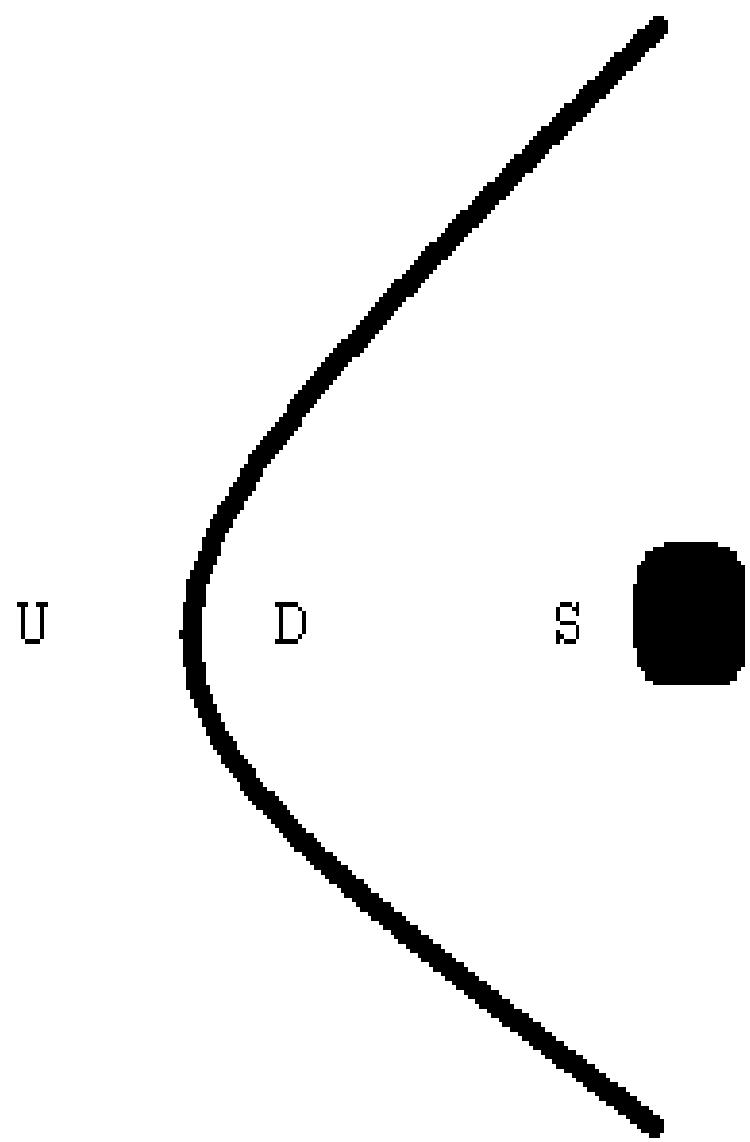
## APPLICATION: SHOCKS DUE TO EXPLOSIONS

Consider an explosion in still air with known pressure and temperature. Let the gas ball pressure be known. The explosion generates a spherical shock wave. Let  $U$  indicate just upstream of the shock and  $D$  indicate just downstream of the shock. In a reference frame moving with the shock, the still air seems to approach at a supersonic speed. With known air and gas pressures, the normal shock equation gives the Mach Number  $M_U$  of the shock. With the still air temperature  $T_U$  known, one can calculate the sound speed front of the shock. This allows us to calculate the shock speed  $U_U$ . The Mach Number connection gives the Mach Number  $M_D$  downstream relative to the shock. The temperature ratio equation gives the temperature  $T_D$  downstream of the shock. This allows us to calculate the sound speed  $C_D$  there. With known Mach Number and sound speed, one can calculate the flow speed  $U_D$  relative to the shock. The absolute flow speed  $U_A$  downstream is equal to the shock speed  $U_U$  minus the flow speed  $U_D$  downstream relative to the shock. This is known as the drift speed. It is a supersonic speed.



#### APPLICATION: BLUNT OBJECT IN SUPERSONIC FLOW

Consider a blunt object in a supersonic flow. A bow shock wave forms upstream of the object. Directly in front of the object this shock wave is a normal shock wave. Let  $U$  indicate just upstream of the shock and  $D$  indicate just downstream of the shock. Let  $S$  indicate the stagnation point on the object. Assume that the pressure  $P_U$  and temperature  $T_U$  upstream of the shock are known and that the Mach Number  $M_U$  of the shock is also known. One can use the pressure ratio equation for a normal shock wave to find the pressure  $P_D$  just downstream of the shock. One can then use the pressure ratio equation for isentropic flow to get the pressure  $P_S$  at the stagnation point. One can use the temperature ratio equation from upstream to the stagnation point to get the temperature  $T_S$  at the stagnation point.



#### APPLICATION: SUPERSONIC FLAT PLATE FOIL

Consider a supersonic flat plate foil moving at a known Mach Number through still air with known pressure and temperature. When the foil has a moderate angle of attack, an oblique shock wave forms below it and an expansion wave forms above it. These turn the flow parallel to the plate. Let  $U$  indicate conditions upstream of the foil. Let  $T$  indicate conditions top of the foil and  $B$  indicate conditions bottom of the foil. One can use the expansion wave plot to find the Mach Number  $M_T$  on top of the foil. With known Mach Number there and upstream of the foil, the isentropic pressure ratio equation gives the pressure  $P_T$  there. One can use the oblique shock plot to find the shock angle  $\beta$ . One can use this to get the Mach Number  $N_U$  of the normal component of the flow. Substitution into the pressure ratio equation for oblique shock waves then gives the pressure  $P_B$  below the foil. With pressure top and bottom of the foil known, one can then calculate the lift.

